# MANIPULATIVES AND CREATIVITY 

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## Epistemology and Sense

$\square$ Senses are physiological capacities of organisms that provide data for perception (Wikipedia, 2013)
$\square$ Five senses: hearing, sight, touch, taste, and smell
$\square$ Other senses: balance, pain, other internal senses
$\square$ How are senses related to students' epistemology?

## Senses for Epistemology

Interwoven and interrelated senses and their synergic effects on students' epistemology


## How to enact creativity education?

 Senses?
## Hearing



## How to enact creativity education? Contents?



## Detailed Course Schedules

- Week 1: Classroom rules
- Week 2-5:
\& creativity
- Week 6-7: Discussion \& field experience
- Week 8-9: Manipulative \& creativity
- Week 9-10: Field experience \& discussion
- Week 11-12: Representation \& creativity
- Week 13: Discussion
- Week 13-15: Group presentation
- Week 16: Survey


## What are manipulatives?

$\square$ Manipulatives is any of various objects or materials that students can touch and move around in order to help them learn mathematical and other concepts (Dictionary.com, 2013)
$\square$ Manipulatives is any of physical objects to support (develop or reinforce) students' mathematical thinking

## Why manipulatives?

$\square$ Students' active engagement in learning process (by physical movement and interests)

- From the concrete to the abstract level
$\square$ From the semiconcrete (representation of a real situation) to the semiabstract (symbolic representation of concrete items) (Heddens, 1986)
- From knowing to doing


## Learning and the use of manipulatives

 (Adding it up, 2001)$\square$ Manipulatives should be considered as not an end, but as a means in themselves.
$\square$ Students need sufficient time to build meaning and make connections.
$\square$ It can be a challenge for students to see mathematical ideas in them (manipulatives).

## Learning and the use of manipulatives

 (Adding it up, 2001)$\square$ Manipulatives also help students correct their own errors.
$\square$ If students do not see the connections among object, symbol, language, and idea, using a manipulatives becomes just one more thing to learn rather than a process learning to a larger mathematical learning goal.

# First Example of manipulatives (Sums of interior and exterior angles) 

$\square$

From WWW.mathlove.co.kr

Second Example of manipulatives (circular cone $=1 / 3 \times$ circular cylinder) (pyramid $=1 / 3 \times$ prism in volume)
from www.mathlove.co.kr

## Third Example of manipulatives (Pythagorean Theorem)

from www.mathlove.co.kr
$\square$ Paper folding from MATHEMATICA 1: The Pythagorean theorem

Fourth Example of manipulatives

$$
(a-b)^{2}=a^{2}-2 a b+b^{2}
$$

미 김유정

## Reference

$\square$ Heddens, J. (1986). Bridging the gap between the concrete and the abstract. Arithmetic Teacher, 33(6), 14-17.
$\square$ Kilpatrick, J., Swafford, J., \& Findell, B. (Eds.). (2001). Adding It Up: Helping Children Learn Mathematics. Washington, DC: National Academies Press.
Q\&A

