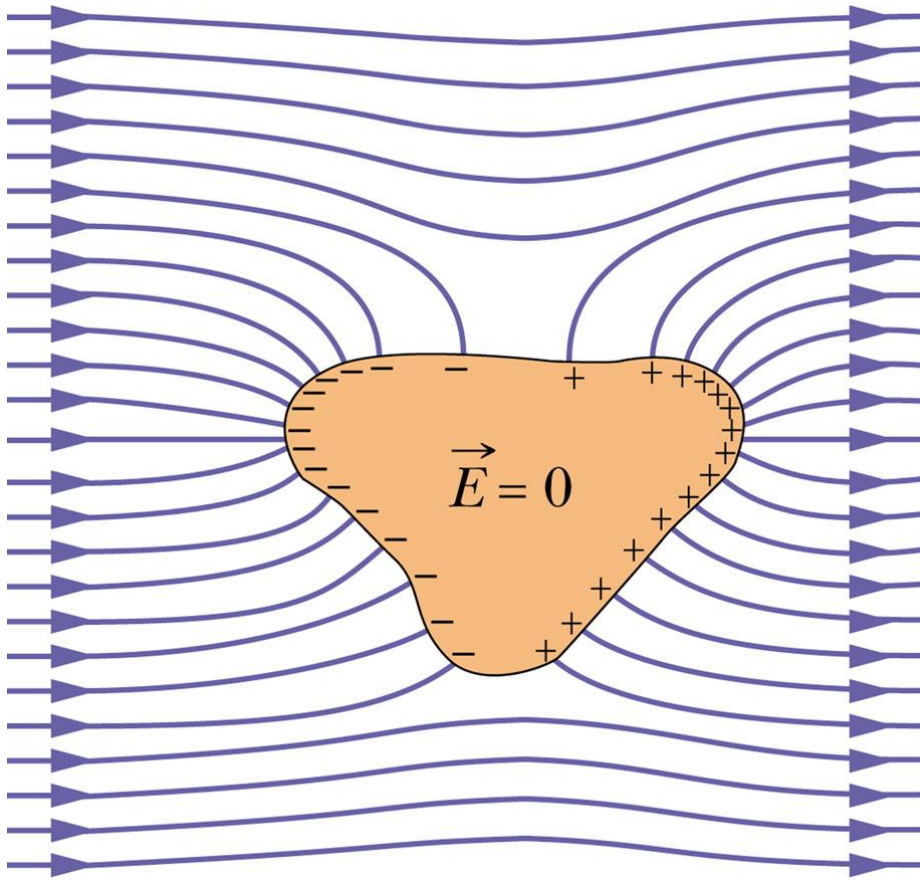


# Copyright statement

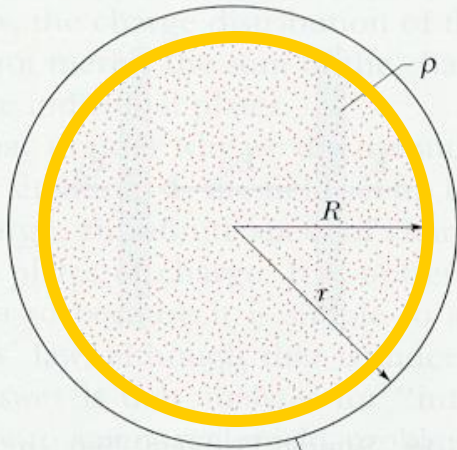
- The images and the pictures in this lecture are provided by the CDs accompanied by the books
  1. University Physics, Bauer and Westfall, McGraw-Hill, 2011.
  2. Principles of Physics, Halliday, Resnick, and Walker, Wiley, 8<sup>th</sup> and 9<sup>th</sup> Ed.
- The rest is made by me.

# Isolated conductor in an external E

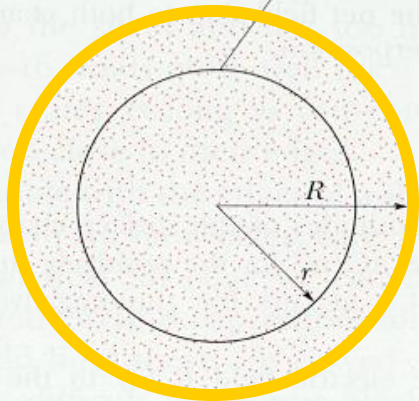


Surface of a conductor is an equipotential surface, hence normal to the electric field.

# Insulating sphere



(a) Gaussian surface

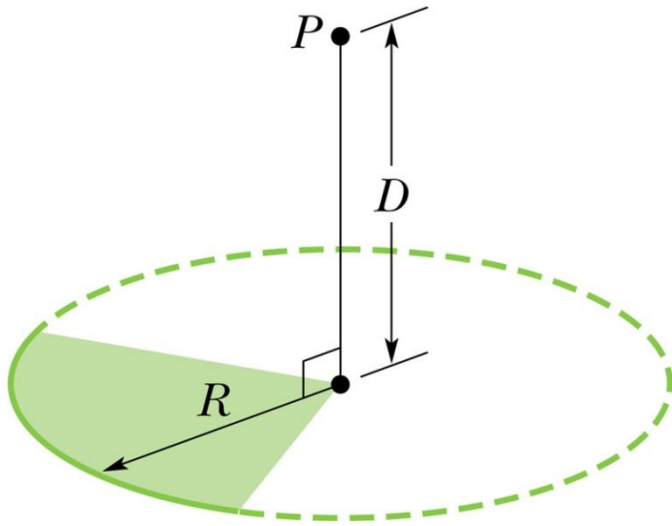


(b)

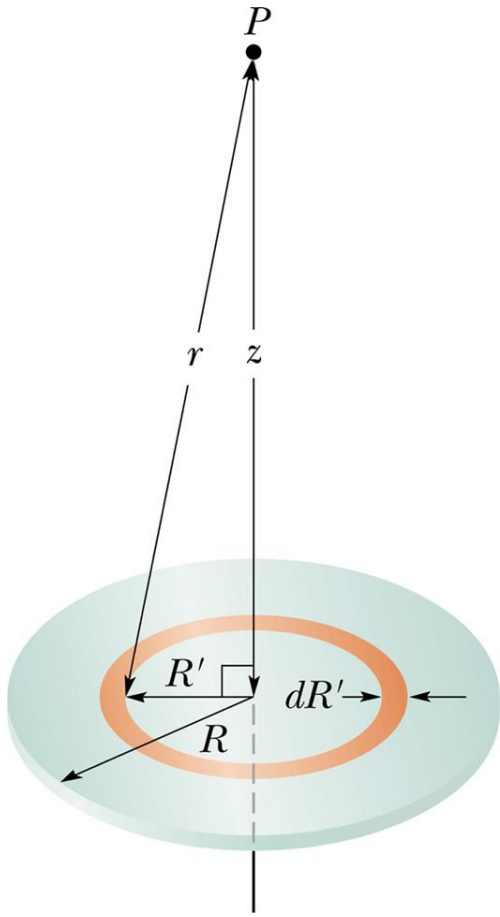
$$r > R; \quad E = \frac{1}{4\pi\epsilon_0} \frac{q}{r^2}$$

$$r < R, \quad E = \frac{1}{4\pi\epsilon_0} \frac{q}{R^3} r$$

# Problem 1



# Surface charge



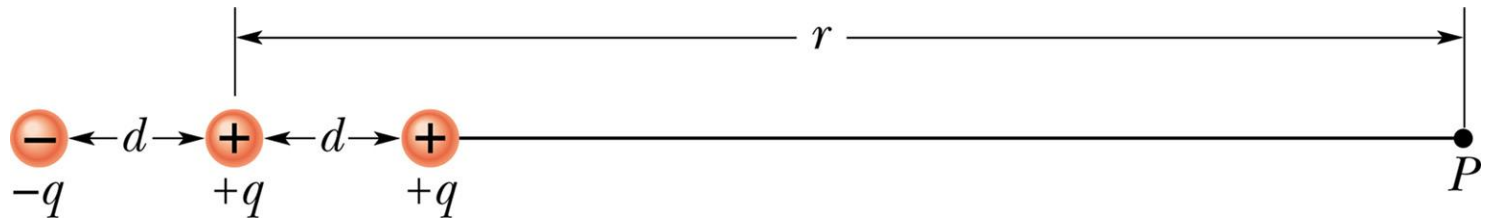
$$V = \frac{\sigma}{2\epsilon_0} \left( \sqrt{z^2 + R^2} - z \right)$$

반지름  $R$ 인 부도체 구에 전하  $q$ 가 균일하게 분포되었을 때의 퍼텐셜에너지는?

$$U = \frac{1}{4\pi\epsilon_0} \frac{3q^2}{5R}$$

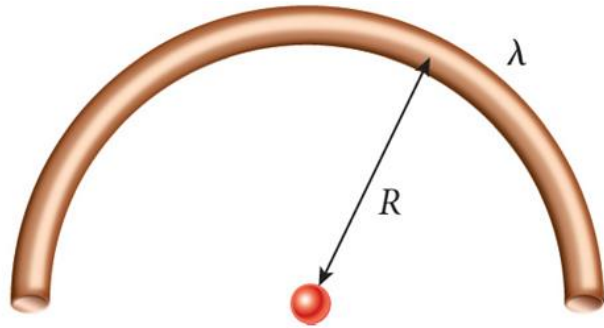


# Problem 2

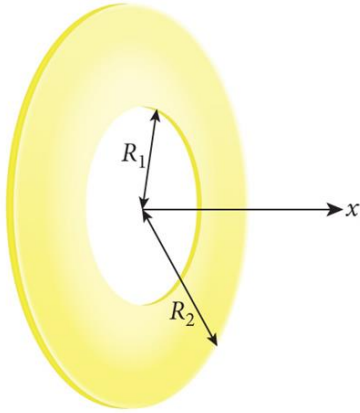




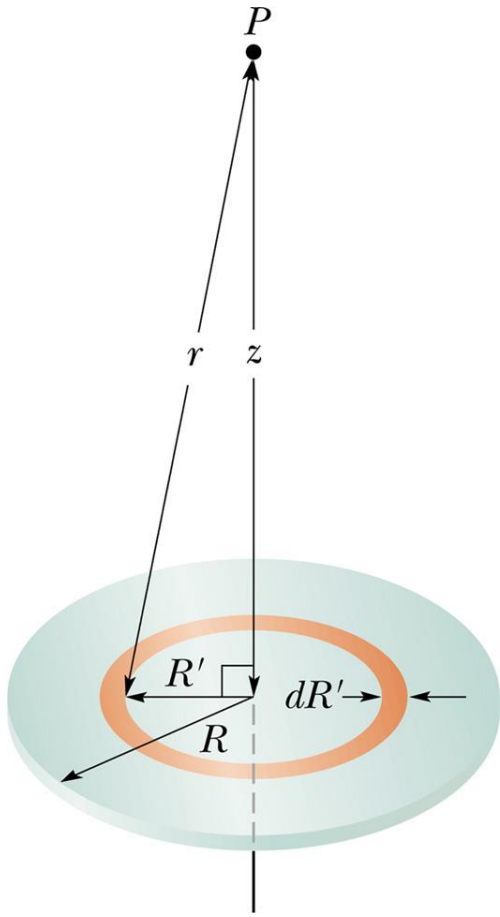
# Problem 3



# Problem 4

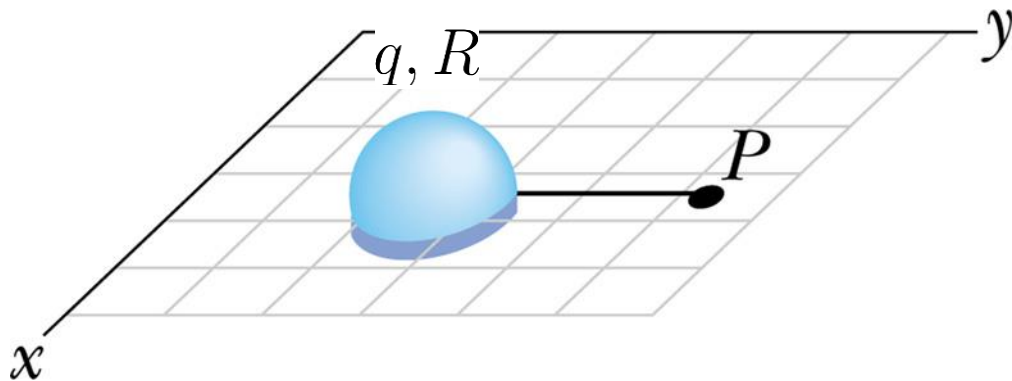


# Surface charge



$$V = \frac{\sigma}{2\epsilon_0} \left( \sqrt{z^2 + R^2} - z \right)$$

# Problem 5



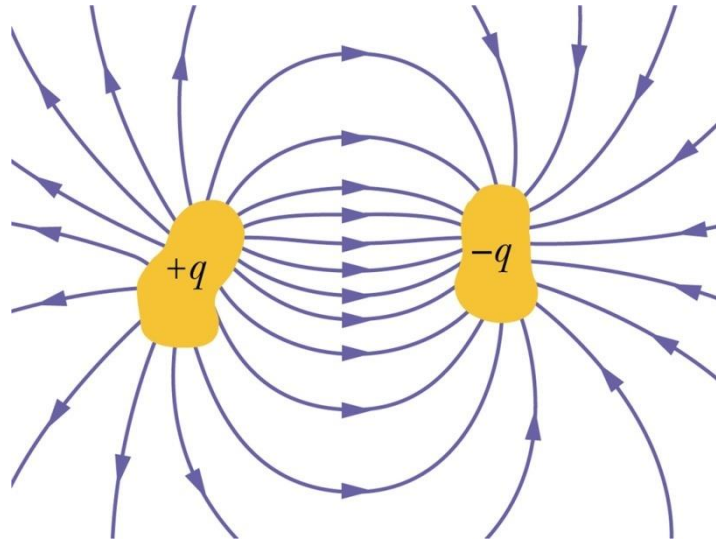
# Chap 24. Capacitors



# Topics in chapter 24

- (1) Concepts of capacitor and capacitance
- (2) Computation of capacitance: parallel plate, cylinder, circle, sphere
- (3) parallel and series connections of capacitors
- (4) Calculation of the electric energy stored in a capacitor:  
energy density of an electric field
- (5) Capacitor with dielectric material:  
electric property of dielectric material and dielectric constant

# Capacitance



Capacitor

전기적으로 고립되어 있는 떨어져 있는 두 도체

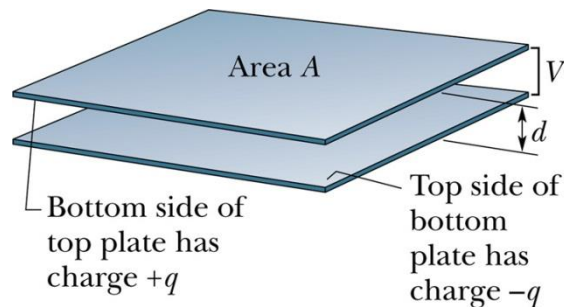
$$q = CV$$

$C$  capacitance

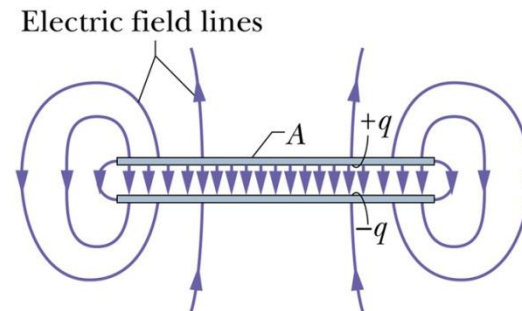
SI unit

1 farad = 1 F = 1 C/V

1. Electric charges reside on the surface.
2. Conductor surfaces are equipotential surfaces.



(a)



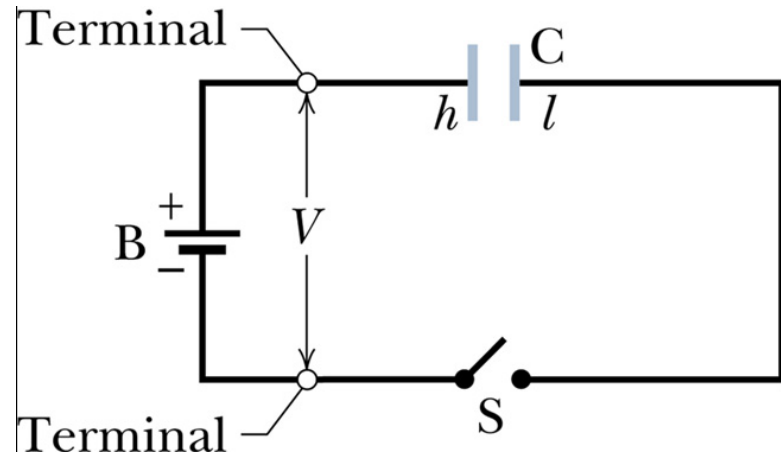
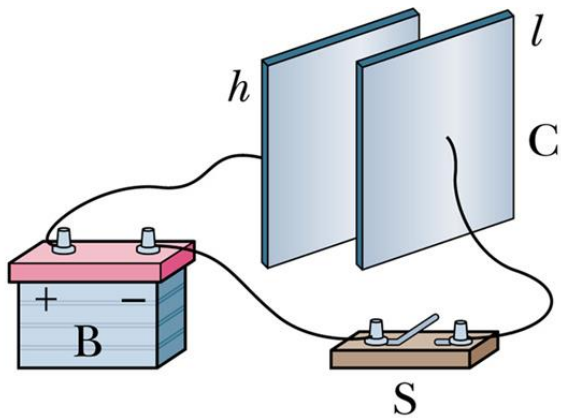
(b)

Electric capacitance can be always written in a form  $C = \epsilon_0 L$ .

$$\epsilon_0 = 8.85 \times 10^{-12} \text{C}^2/\text{N} \cdot \text{m}^2$$

This can be written as follows:

$$\epsilon_0 = 8.85 \times 10^{-12} \text{F}/\text{m} = 8.85 \text{pF}/\text{m}$$





# Computation of capacitance

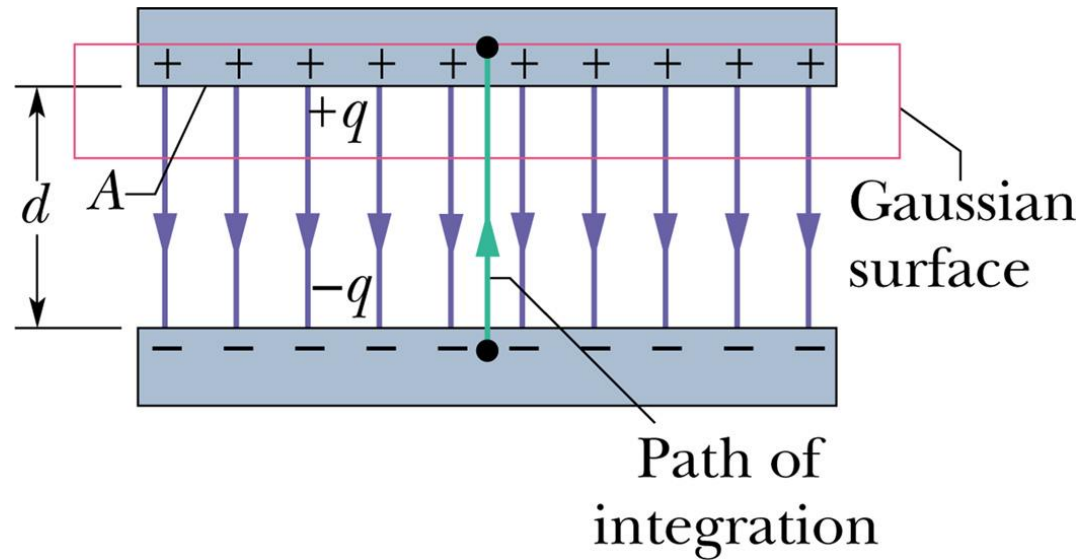
1. 도체 한 쪽에 전하  $q$ , 다른 쪽에 전하  $-q$ 를 놓는다.
2. 두 전하 사이의 electric field를 계산한다.
3. Potential difference를 구한다.

Electric field  $\epsilon_0 \oint \vec{E} \cdot d\vec{A} = q$

Electric potential difference  $V_f - V_i = - \int_i^f \vec{E} \cdot d\vec{s}$

$$C = \frac{q}{|\Delta V|}$$

# Parallel capacitor

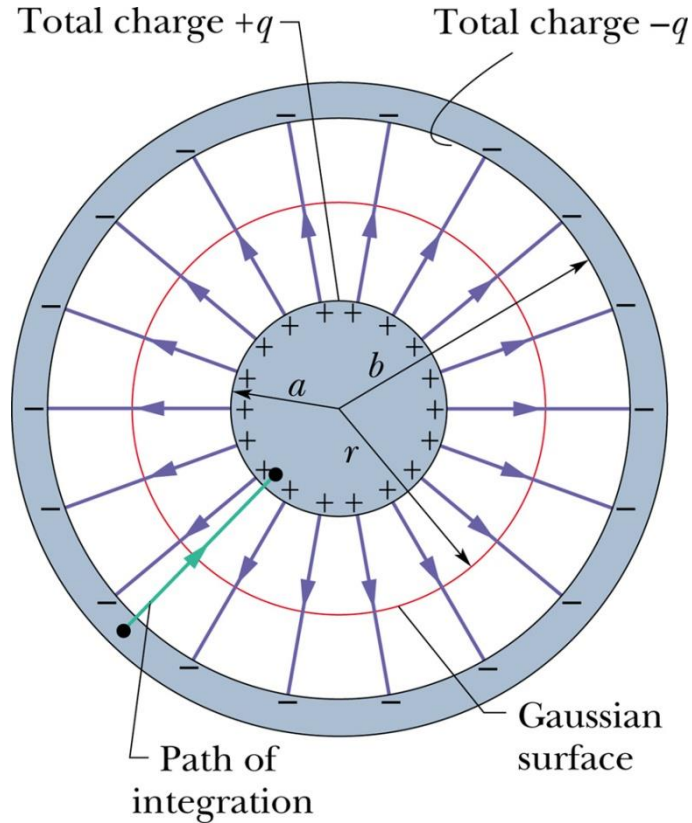


$$\epsilon_0 \oint \vec{E} \cdot d\vec{A} = q \quad \longrightarrow \quad q = \epsilon_0 E A$$

$$V_f - V_i = - \int_i^f \vec{E} \cdot d\vec{s} \quad \longrightarrow \quad V = \int_-^+ E ds = E \int_-^+ ds = E d$$

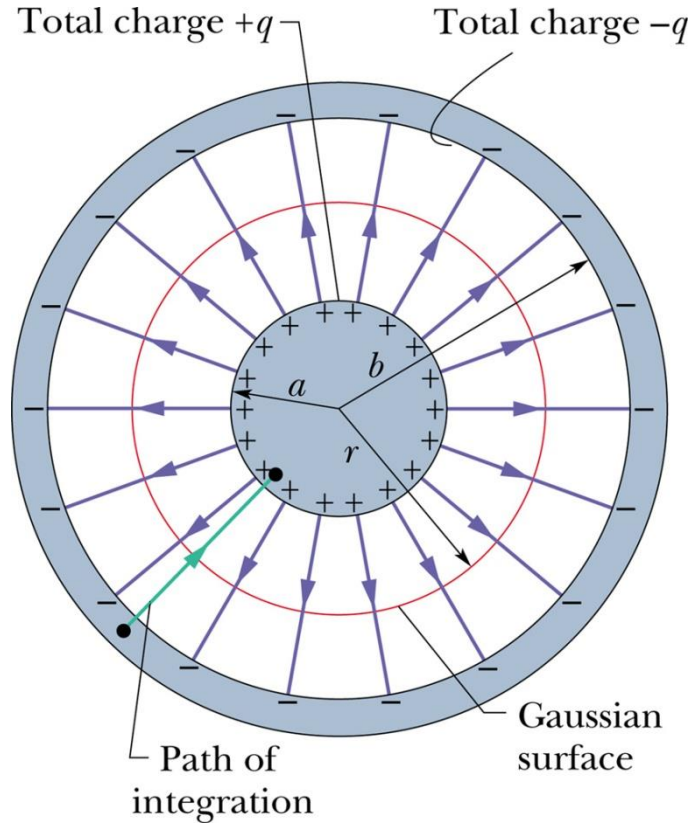
$$C = \frac{\epsilon_0 A}{d}$$

# Cylindrical capacitor



$$C = 2\pi\epsilon_0 \frac{L}{\ln(b/a)}$$

# Spherical capacitor



$$C = 4\pi\epsilon_0 \frac{ab}{b-a}$$

고립된 공  $C = 4\pi\epsilon_0 R$