

LECTURE 2

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3. Basic Current Mirrors and Single-Stage Amplifiers

3.1 Simple CMOS Current Mirrors

3.2 Common-Source Amplifier

3.3 Source-Follower or Common-Drain Amplifier

3.4 Common-Gate Amplifier

3.5 Source-Degenerated Current Mirrors

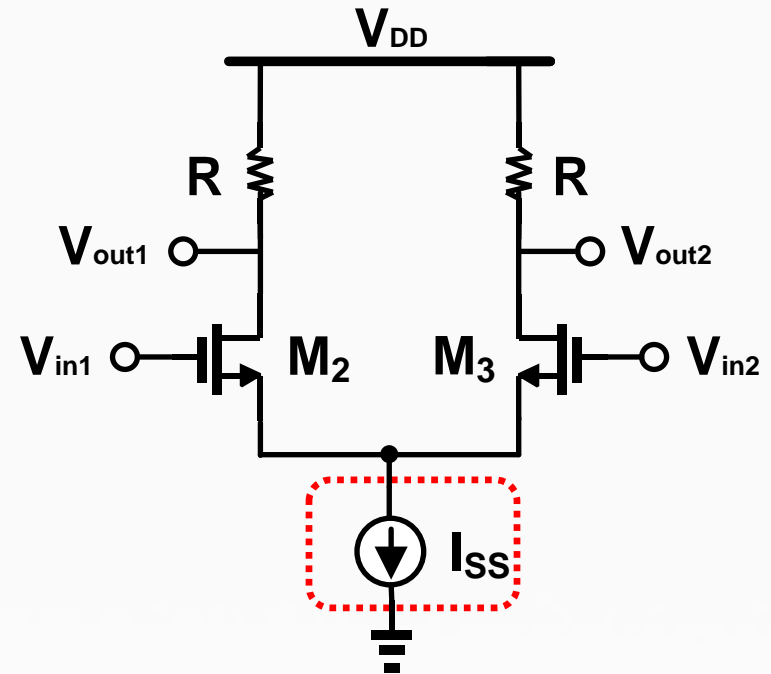
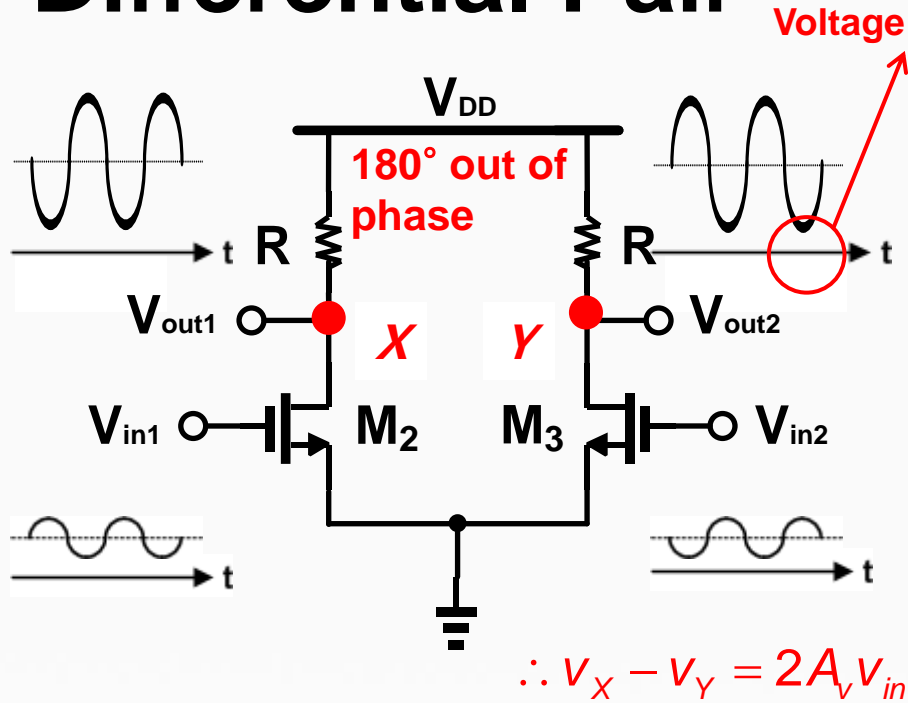
3.6 Cascode Current Mirrors

3.7 Cascode Gain Stage

3.8 MOS Differential Pair and Gain Stage



Differential Pair



Merits

1. High noise rejection
2. High output swings

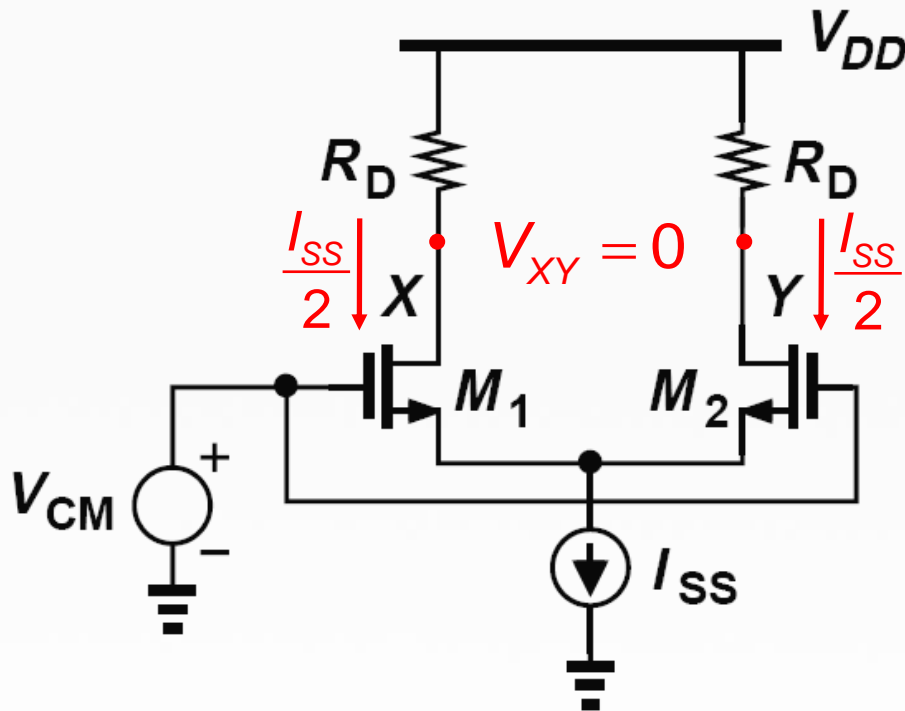


The g_m and the output CM level are varying

Constant current source
(Tail current source)



Common-Mode Response



$$V_{G1} = V_{G2} = V_{CM}, \quad I_{D1} = I_{D2} = \frac{I_{SS}}{2}$$

$$V_X = V_Y = V_{DD} - R_D \frac{I_{SS}}{2}$$

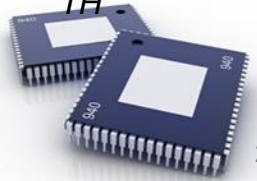
$$V_{out,CM} \Rightarrow V_{XY} = 0$$

For operation in saturation region

$$V_{DS} > V_{GS} - V_{TH}$$

$$V_D > V_G - V_{TH}$$

$$V_{CM} < V_{DD} - R_D \frac{I_{SS}}{2} + V_{TH}$$



Example 1

a) Gain이 5이고 Power consumption이 2mW인 NMOS differential pair를 설계하는데, differential pair를 따르는 단이 적어도 1.6V의 Output CM level을 요구하는 것을 조건으로 한다. $\mu_n C_{ox} = 100\mu A/V^2$, $\lambda = 0$, 그리고 $V_{DD} = 1.8V$ 로 가정한다. 이때 W/L을 구하여라.

Sol) 한계 전력 소모와 V_{DD} 로부터 I_{SS} 를 구한다.

$$I_{SS} = 1.11mA$$

Output CM level은 다음과 같다.

$$V_{CM,out} = V_{DD} - R_D \frac{I_{SS}}{2}$$

$V_{CM,out} = 1.6V$ 를 위해서 계산을 하면 R_D 는 다음과 같다.

$$R_D \leq \frac{2}{I_{SS}}(V_{DD} - 1.6) \rightarrow R_D = 360\Omega$$

$g_m R_D = 5$ 이고, 각 트랜지스터에 $\frac{I_{SS}}{2}$ 가 흐르므로

$$g_m = \sqrt{2\mu_n C_{ox} \frac{W}{L} \frac{I_{SS}}{2}} = \frac{5}{360\Omega}$$

이에 따라서 W/L은 $\frac{W}{L} = 1738$ 가 된다.



Example 1

b) (a)의 예제에서 $V_{TH} = 0.4V$ 라면 허용 가능한 최대 input CM level은 얼마인가?

Sol) $V_{CM,in}$ 은 다음과 같이 정리 할 수 있다.

$$V_{CM,in} < V_{DD} - R_D \frac{I_{SS}}{2} + V_{TH}$$

$V_{CM,out} = V_{DD} - R_D \frac{I_{SS}}{2}$ 이므로 정리하면 다음과 같다.

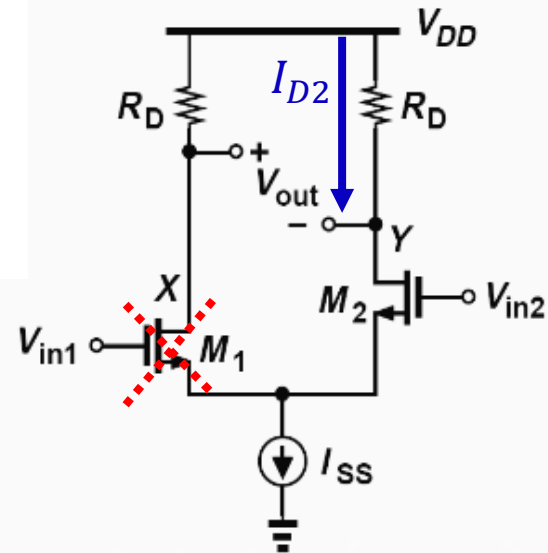
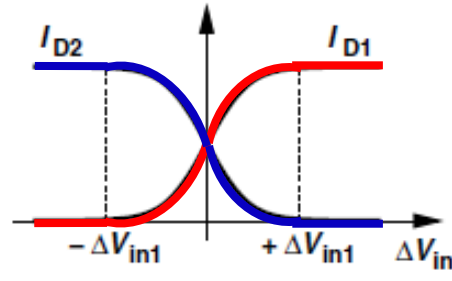
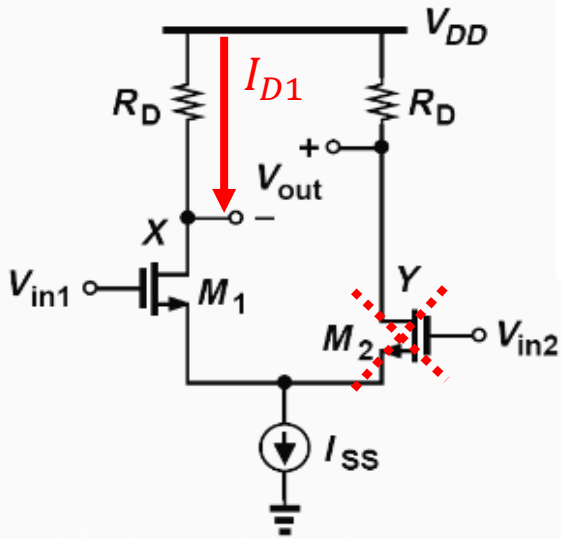
$$V_{CM,in} < V_{CM,out} + V_{TH}$$

$V_{CM,out} = 1.6V$, $V_{TH} = 0.4V$ 이므로

$$V_{CM,in} < 2V$$



Differential Response



$$V_{in1} > V_{in2}$$

$$I_{D1} = I_{SS}$$

$$I_{D2} = 0$$

$$V_X = V_{DD} - R_D I_{SS}$$

$$V_Y = V_{DD}$$

$$V_{in1} < V_{in2}$$

$$I_{D2} = I_{SS}$$

$$I_{D1} = 0$$

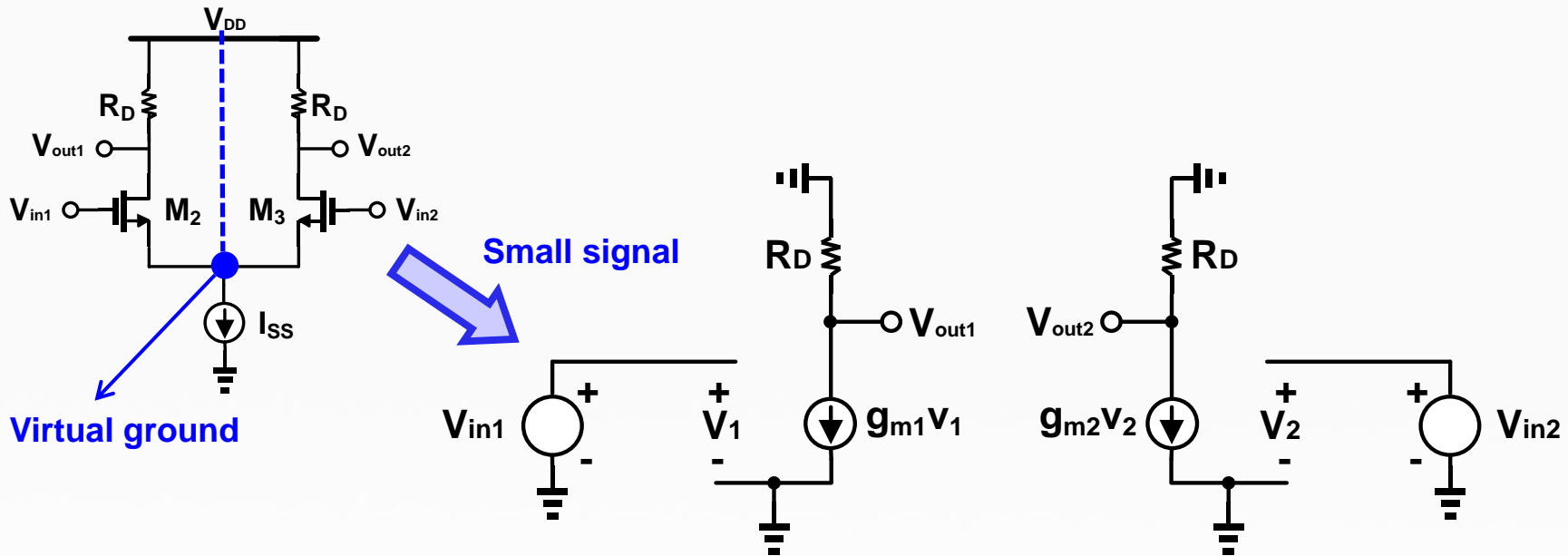
$$V_Y = V_{DD} - R_D I_{SS}$$

$$V_X = V_{DD}$$



Small-Signal Response

❖ Virtual Ground and Half Circuit



$$V_{out1} = -g_{m1}R_D V_{in1}$$

$$V_{out2} = -g_{m2}R_D V_{in2}$$

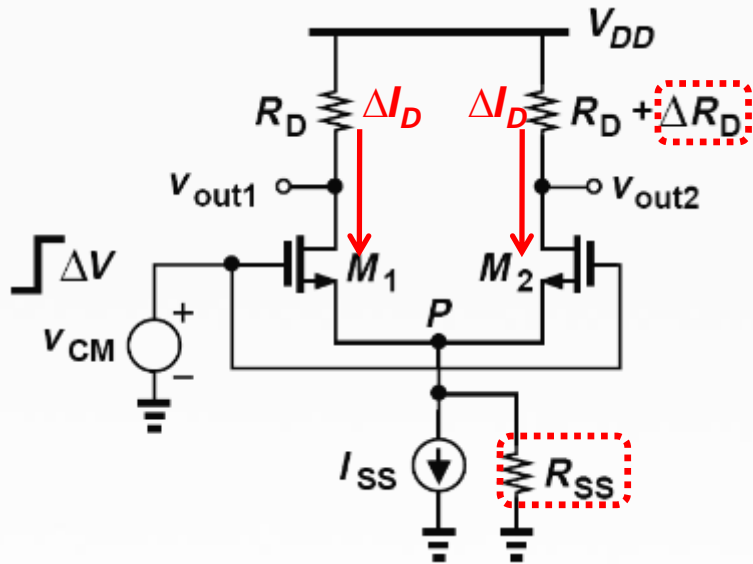


$$A_V = \frac{V_{out1} - V_{out2}}{V_{in1} - V_{in2}} = -g_{m1,2}R_D$$



CM to DM Conversion, A_{CM-DM}

Asymmetric loads (ΔR_D)



$$\Delta V_{CM} = \Delta V_{GS} + 2\Delta I_D R_{SS}$$

$$\text{since } \Delta V_{GS} = \Delta I_D / g_m,$$

$$\Delta V_{CM} = \Delta I_D (1/g_m + 2R_{SS})$$

$$\Delta I_D = \frac{\Delta V_{CM}}{1/g_m + 2R_{SS}}$$

$$\begin{aligned} \Delta V_{out} &= \Delta V_{out1} - \Delta V_{out2} \\ &= \Delta I_D R_D - \Delta I_D (R_D + \Delta R_D) \\ &= -\Delta I_D \Delta R_D \end{aligned}$$

$$= -\frac{\Delta V_{CM}}{1/g_m + 2R_{SS}} \Delta R_D$$

$$\therefore |A_{CM-DM}| = \left| \frac{\Delta V_{out}}{\Delta V_{CM}} \right| = \frac{\Delta R_D}{\frac{1}{g_m} + 2R_{SS}}$$

In ideal case,

$$R_{SS} \rightarrow \infty,$$

$$\Delta R_D \rightarrow 0,$$

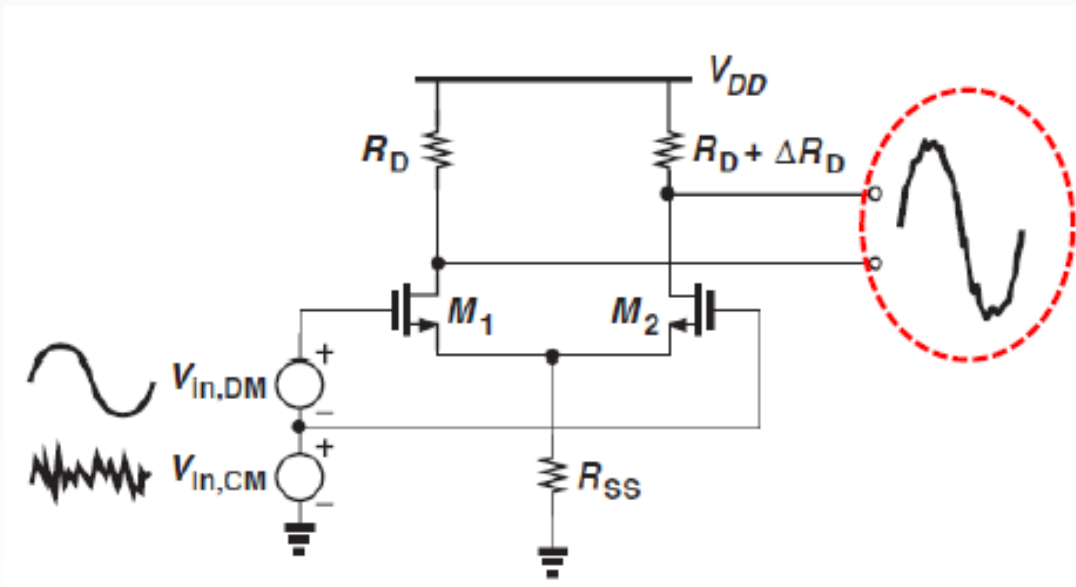
$$\therefore A_{CM-DM} = 0$$



CMRR

Common-mode rejection ratio (CMRR)

: Input의 **Common noise의 Variation**이 얼마나 **output**에서 **제거**되는가



$$CMRR = \left| \frac{A_{DM}}{A_{CM-DM}} \right|$$
$$= \frac{g_m \cdot R_D}{\frac{1}{g_m} + 2R_{SS}}$$

In ideal case

$$A_{CM-DM} = 0,$$

$$\therefore CMRR \rightarrow \infty$$



Example 2

$W_3 = 10\mu m, W_4 = 11\mu m$ 일 때 CMRR를 구하여라.

Sol) CMRR은 다음과 같이 정리 할 수 있다.

$$CMRR = \frac{g_m \cdot R_D}{\frac{1}{g_m} + 2R_{SS}} = \frac{1 + 2g_{m1}R_{SS}}{\frac{\Delta R_D}{R_D}}$$

$M_{3,4}$ 는 R로 바꾸어주면 다음과 같다.

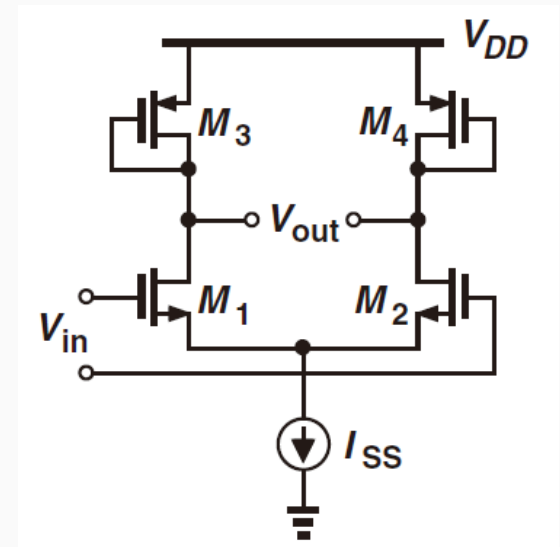
$$R_{D1} = \frac{1}{g_{m3}}, R_{D2} = \frac{1}{g_{m4}}$$

R 값이 위와 같을 때 Miss match를 계산해주면,

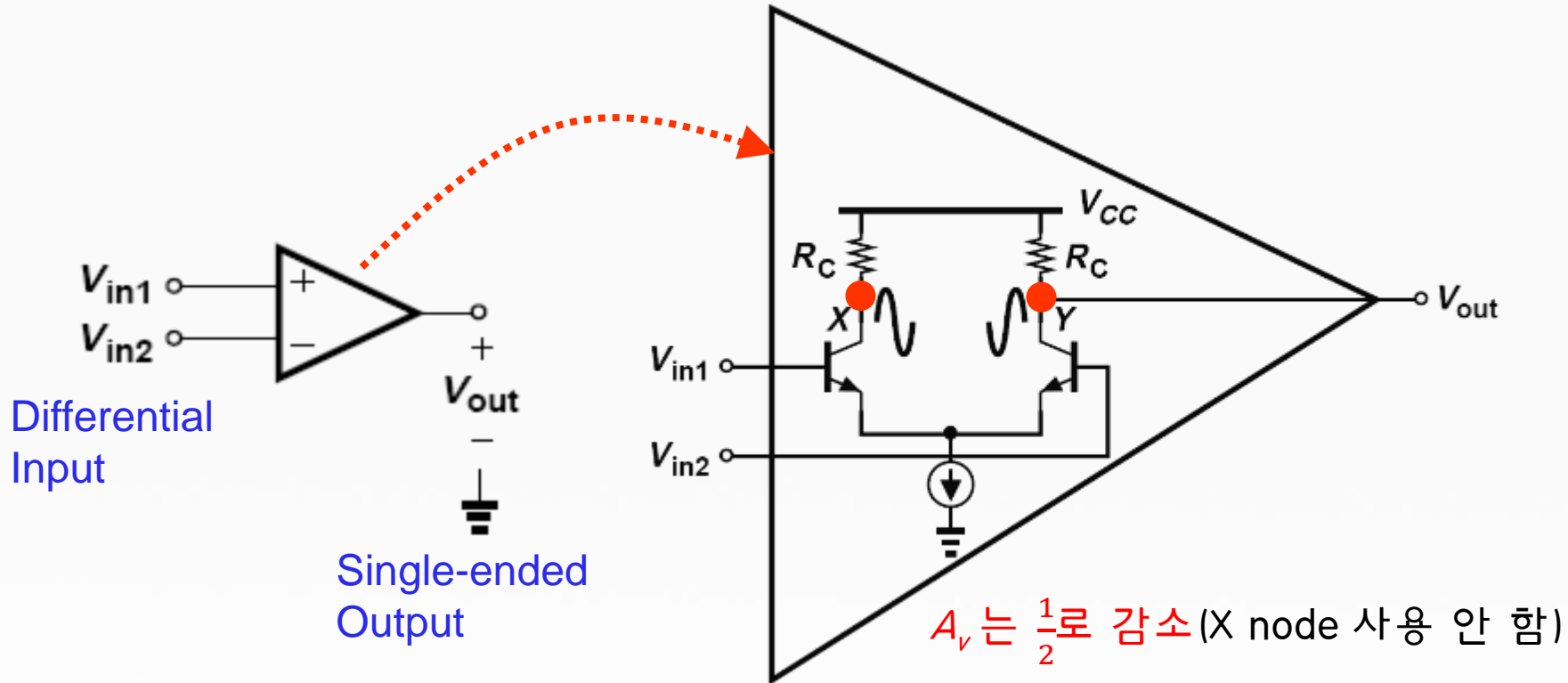
$$\frac{\Delta R_D}{R_D} = \frac{R_{D1} - R_{D2}}{R_{D1}} = 1 - \frac{R_{D2}}{R_{D1}} = 1 - \frac{g_{m3}}{g_{m4}} = 1 - \frac{\sqrt{2\mu_p C_{ox} \left(\frac{W}{L}\right)_3 I_D}}{\sqrt{2\mu_p C_{ox} \left(\frac{W}{L}\right)_4 I_D}} = 1 - \sqrt{\frac{10}{11}} = 0.0465$$

위의 CMRR의 수식에 대입을 하면,

$$CMRR = 2248$$



Differential to Single-ended Conversion

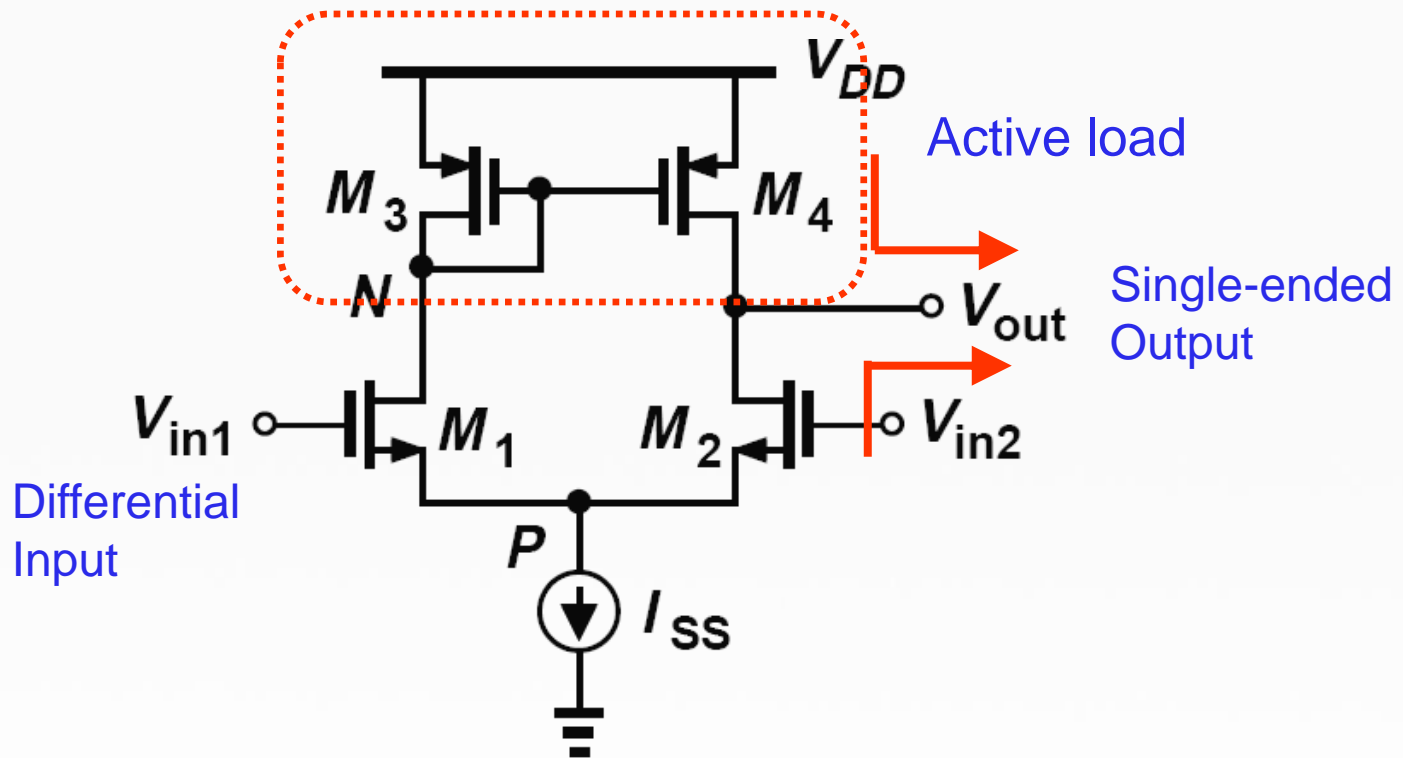


Many circuits **require a differential to single-ended conversion**, however, the above topology is not very good. (A_v 감소)



Better Alternative

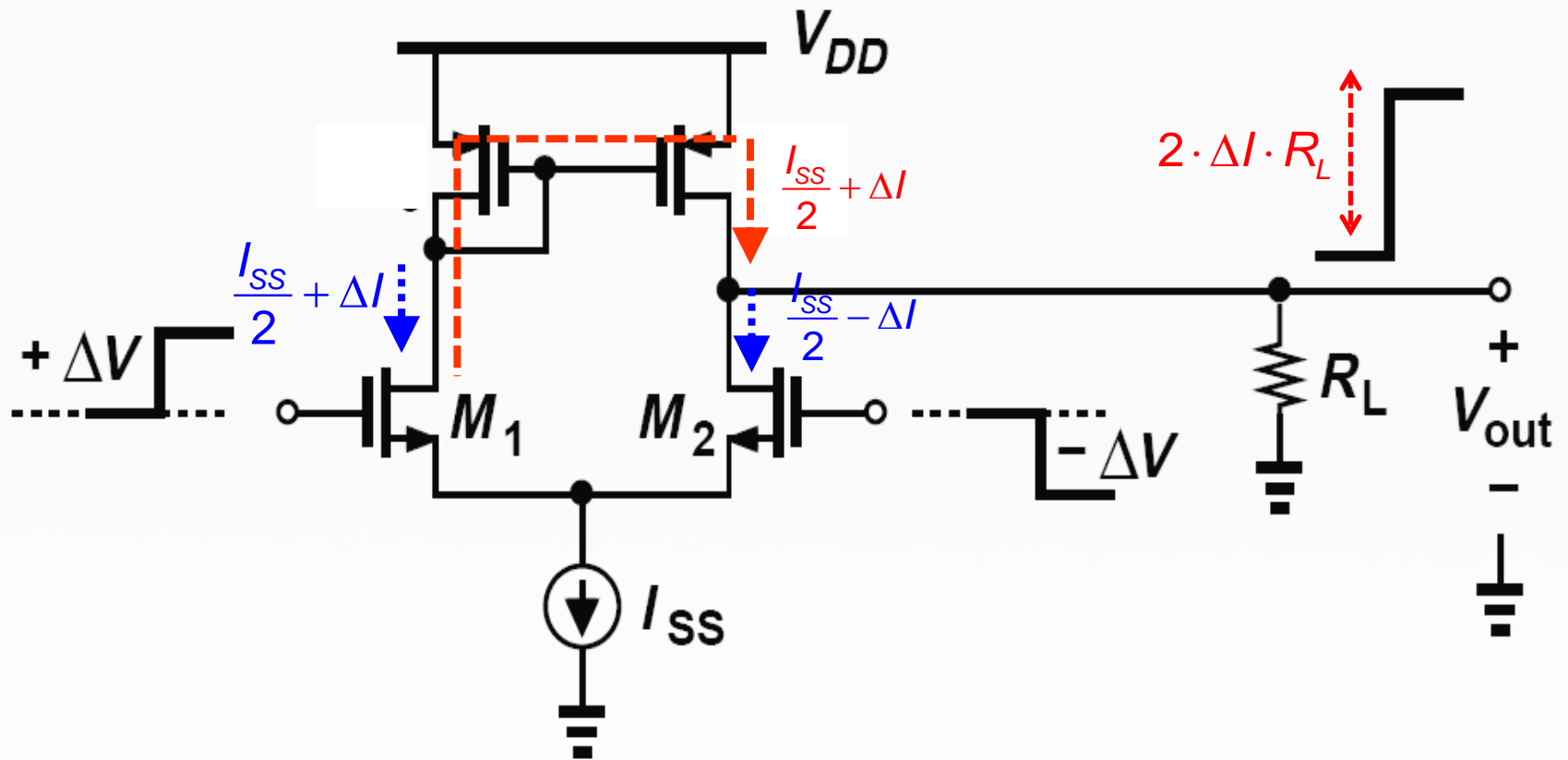
❖ Active load – Current mirror



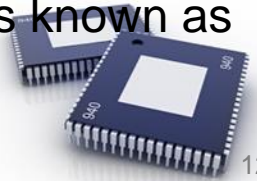
This circuit topology performs differential to single-ended conversion **with no loss of gain**.



MOS Differential Pair with Active Load

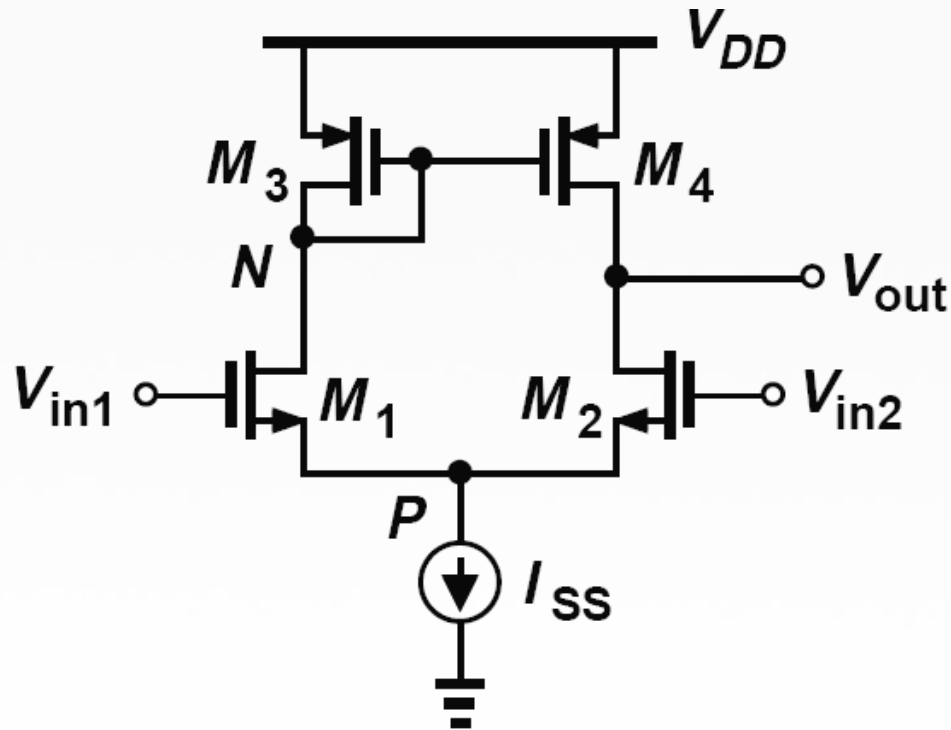


This type of load is different from the conventional “static load” and is known as an “**active load**”.



How are the gain calculated?

- ❖ Gain? -> half circuit (Asymmetric load)
- > ① Small signal
- ② Thevenin equivalent



Use the small signal

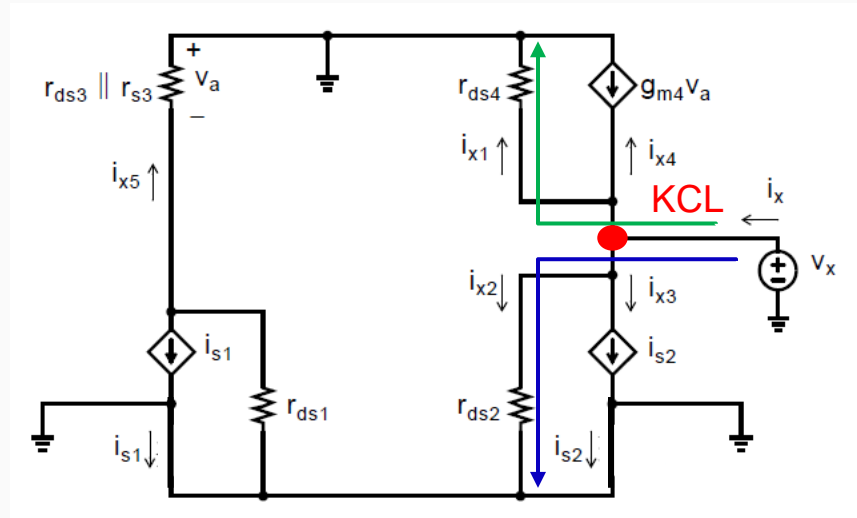
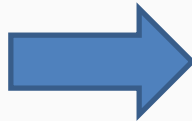
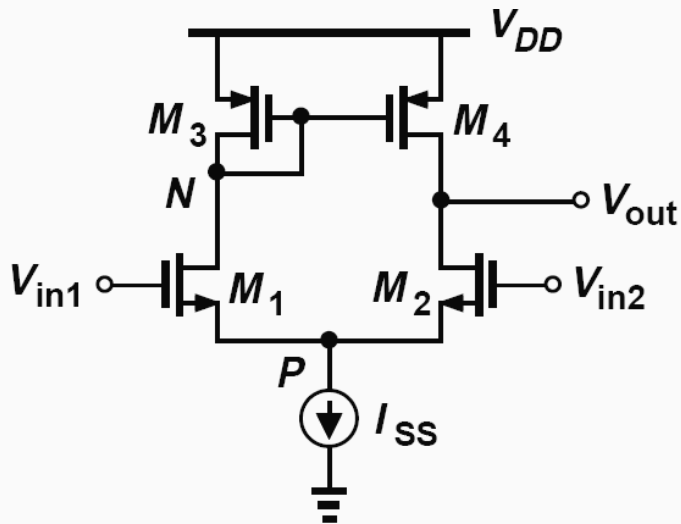


Fig. 3.20 The small-signal model

Use the KCL

$$i_X = i_{X1} + i_{X2} + i_{X3} + i_{X4}$$

$$i_{X1} = \frac{V_X}{r_{ds4}} \quad i_{X2} = \frac{V_X}{r_{ds2}} \quad (3.73, 3.74)$$

Current mirror

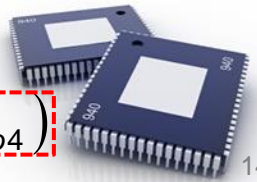
$$i_{X4} = i_{X5} = -i_{S1} = -i_{S2} = -i_{X3} \quad (3.76)$$

$$r_{out} = \frac{V_X}{i_X} = \frac{V_X}{i_{X1} + i_{X2} + i_{X3} + i_{X4}} = \frac{V_X}{\left(\frac{V_X}{r_{ds4}}\right) + \left(\frac{V_X}{r_{ds2}}\right)} \quad (3.77)$$

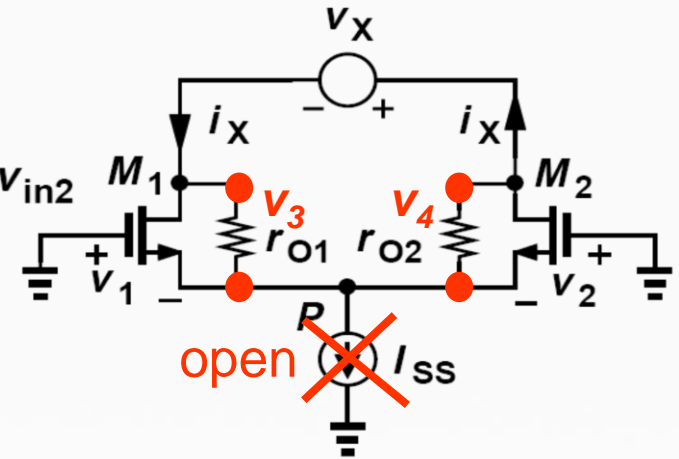
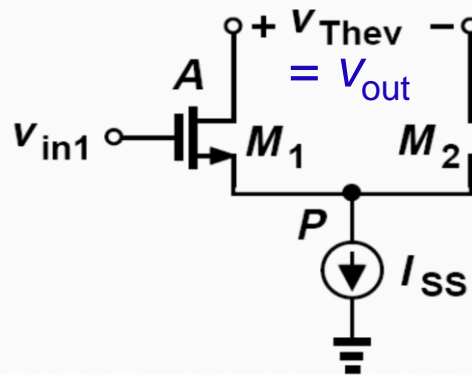
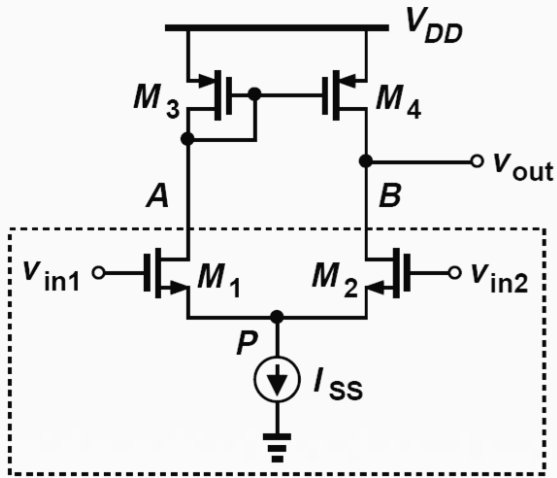
$$r_{out} = r_{ds2} \parallel r_{ds4} \quad (3.78)$$

$$i_{S1} = i_{S2} = -\frac{V_X}{2r_{ds2}} \quad (3.75)$$

$$A_V = g_m r_{out} = g_{m1} (r_{ds2} \parallel r_{ds4}) = g_{m1} (r_{o2} \parallel r_{o4}) \quad (3.79)$$



V_{Thev} and R_{Thev}



$$\therefore V_{Thev} = -g_m r_{oN} (v_{in1} - v_{in2})$$

$$v_3 + v_4 = v_X$$

$$(i_X - g_{m1} v_1) r_{O1} + (i_X + g_{m2} v_2) r_{O2} = v_X$$

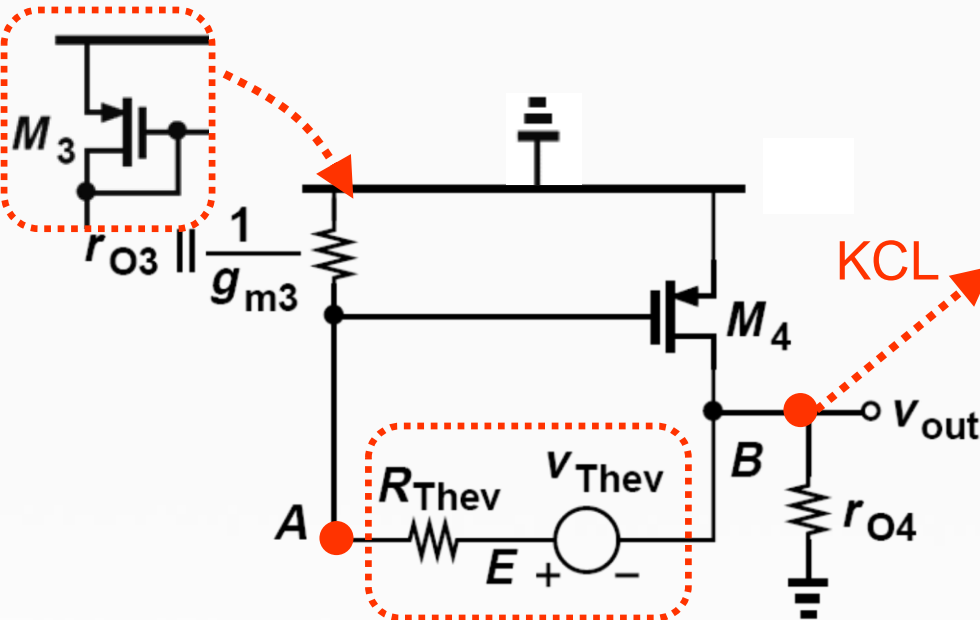
since $v_1 = v_2$, $g_{m1} = g_{m2}$, $r_{O1} = r_{O2} = r_{oN}$

$$i_X r_{oN} + i_X r_{oN} = v_X$$

$$\therefore R_{Thev} = \frac{v_X}{i_X} = 2r_{oN}$$



Simplified Differential Pair with Active Load



$$v_A = \frac{1/g_{m3} \parallel r_{O3}}{1/g_{m3} \parallel r_{O3} + R_{Thev}} (v_{out} + v_{Thev})$$

$$-g_{m4}(-v_A) + \frac{v_{out}}{r_{O4}} + \frac{v_{out} + v_{Thev}}{1/g_{m3} \parallel r_{O3} + R_{Thev}} = 0$$

since $1/g_{m3} \ll r_{O3}, 1/g_{m3} \ll R_{Thev},$

$$g_{m3} = g_{m4} = g_{mp}, r_{O3} = r_{O4} = r_{oP}$$

$$\frac{2}{R_{Thev}} (v_{out} + v_{Thev}) + \frac{v_{out}}{r_{oP}} = 0$$

$$v_{out} \left(\frac{1}{r_{oN}} + \frac{1}{r_{oP}} \right) = \frac{g_{mN} r_{oN} (v_{in1} - v_{in2})}{r_{oN}}$$

$$\therefore \frac{v_{out}}{v_{in1} - v_{in2}} = g_{mN} (r_{oN} \parallel r_{oP})$$

$$= \underline{g_{m1,2} (r_{O1,02} \parallel r_{O3,04})}$$

$$\begin{cases} v_{Thev} = -g_m r_{oN} (v_{in1} - v_{in2}) \\ R_{Thev} = 2r_{oN} \end{cases}$$

