

Copyright statement

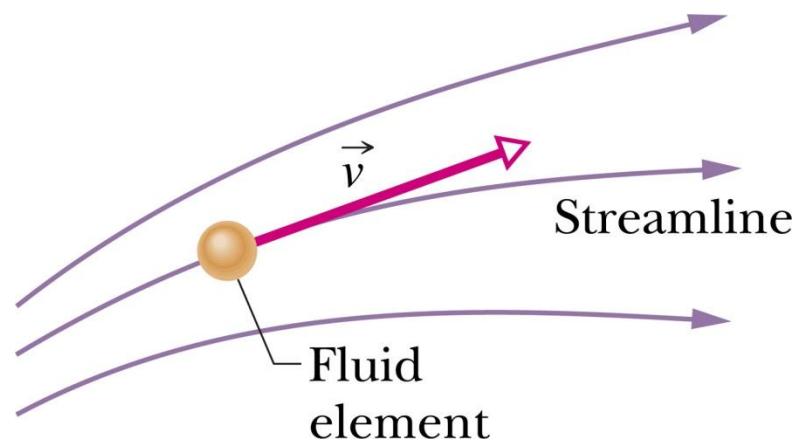
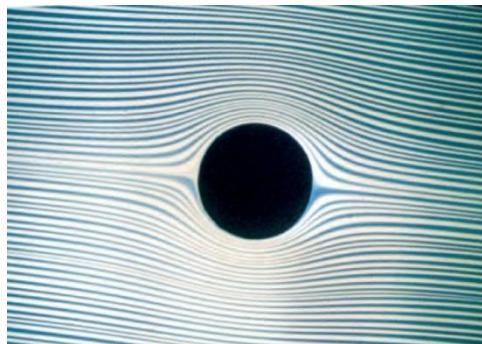
- The images and the pictures in this lecture are provided by the CDs accompanied by the books
 1. University Physics, Bauer and Westfall, McGraw-Hill, 2011.
 2. Principles of Physics, Halliday, Resnick, and Walker, Wiley, 8th and 9th Ed.
- The rest is made by me.

Ideal flow의 운동

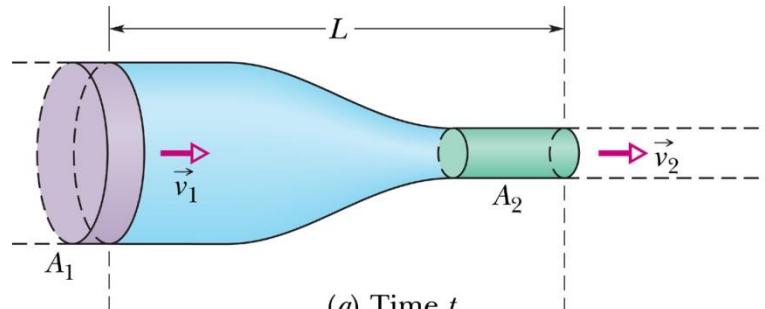


1. steady flow
2. incompressible flow
3. nonviscous flow
4. irrotational flow

streamline



Continuity equation

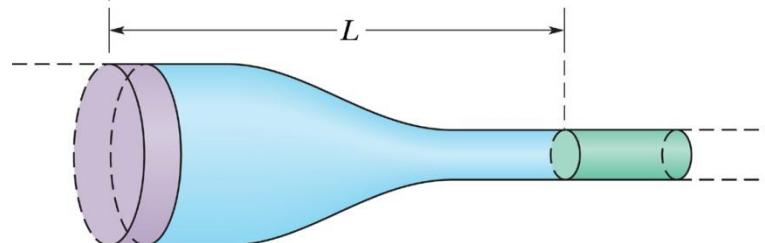


$$\Delta V = A \Delta x = A v \Delta t$$

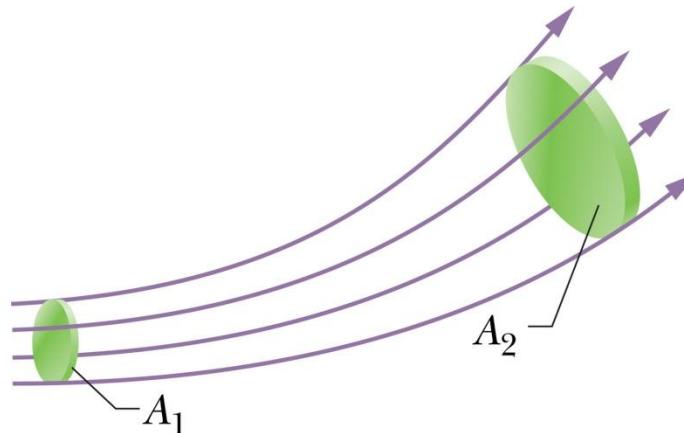
$$\Delta V = A_1 v_1 \Delta t = A_2 v_2 \Delta t$$

$$A_1 v_1 = A_2 v_2$$

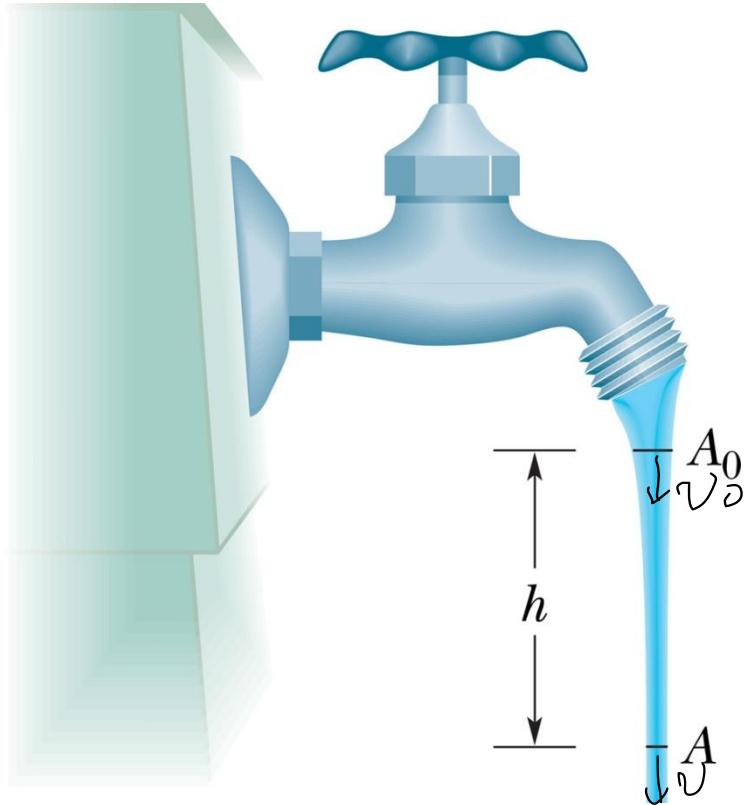
continuity equation



(b) Time $t + \Delta t$



Sample prob.



$$A_0 v_0 = A v$$

$$\frac{A_0^2}{A^2} v_0^2 = v^2 = v_0^2 + 2gh \quad \nearrow v_0 = \sqrt{\frac{2ghA^2}{A_0^2 - A^2}}$$

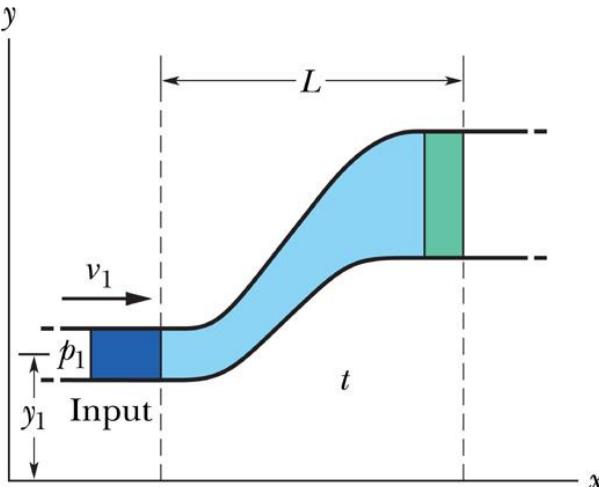
$$v_0 = \sqrt{\frac{2ghA^2}{A_0^2 - A^2}}$$

$$R_V = A_0 v_0 = \sqrt{\frac{2ghA^2}{1 - A^2/A_0^2}}$$

$$A_0 = 1.2 \text{ cm}^2, \quad A = 0.35 \text{ cm}^2, \quad h = 45 \text{ mm}$$

$$v_0^2 \left(\frac{A_0^2 - A^2}{A^2} \right) = 2gh$$

Bernoulli 방정식



$$W = \Delta K$$

$$\Delta K = \frac{1}{2} \Delta m v_2^2 - \frac{1}{2} \Delta m v_1^2 = \frac{1}{2} \rho \Delta V (v_2^2 - v_1^2)$$

$$W_g = -\Delta m g (y_2 - y_1) = -\rho g \Delta V (y_2 - y_1)$$

$$F \Delta x = p A \Delta x = p(A \Delta x) = p \Delta V$$

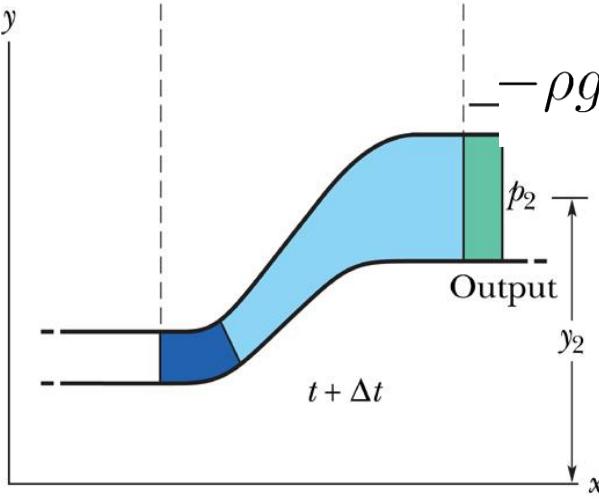
$$W_p = -p_2 \Delta V + p_1 \Delta V = -(p_2 - p_1) \Delta V$$

$$-\rho g \Delta V (y_2 - y_1) - \Delta V (p_2 - p_1) = \frac{1}{2} \rho \Delta V (v_2^2 - v_1^2)$$

$$p_1 + \frac{1}{2} \rho v_1^2 + \rho g y_1 = p_2 + \frac{1}{2} \rho v_2^2 + \rho g y_2$$

$$p + \frac{1}{2} \rho v^2 + \rho g y = \text{const.}$$

Bernoulli 방정식



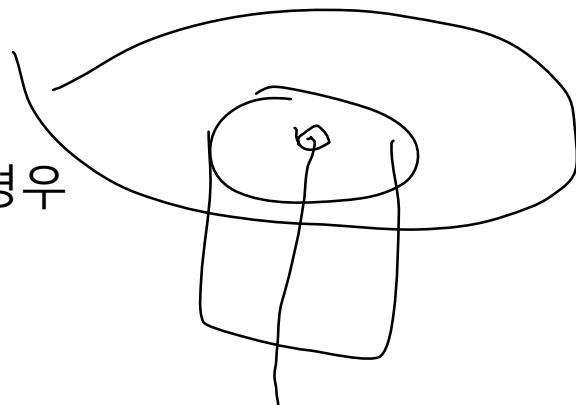
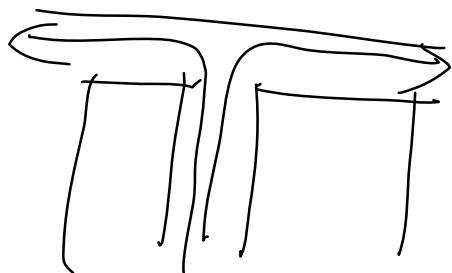
Bernoulli 방정식의 특별한 경우

(1) 정지한 유체 $v_1 = v_2 = 0$

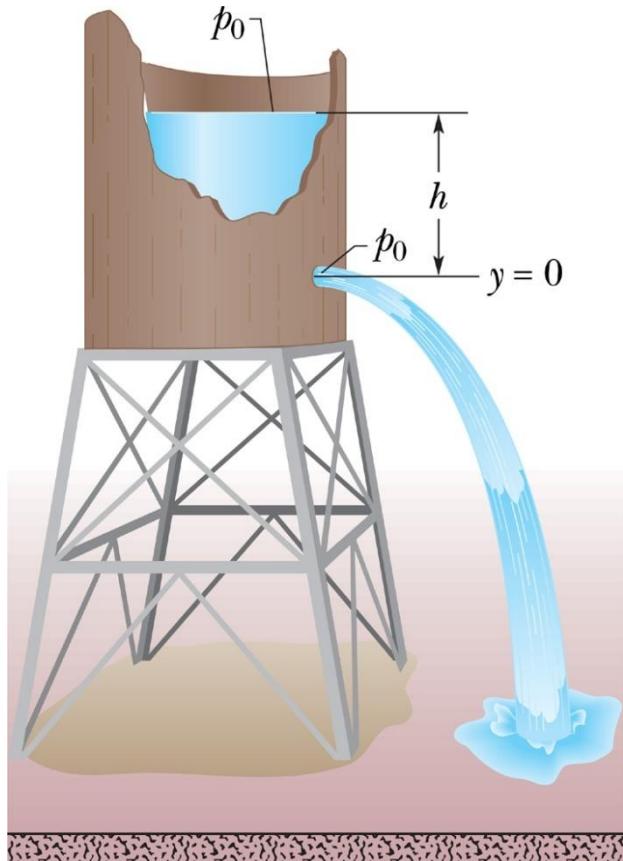
$$p_2 = p_1 + \rho g(y_1 - y_2)$$

(2) 같은 높이의 유체 $p_1 + \frac{1}{2}\rho v_1^2 = p_2 + \frac{1}{2}\rho v_2^2$

- 예: 1) 차창 밖으로 나가는 담배연기
2) 바람 부는 날 문이 세게 닫히는 경우
3) 실패로 만든 장난감



Sample prob.

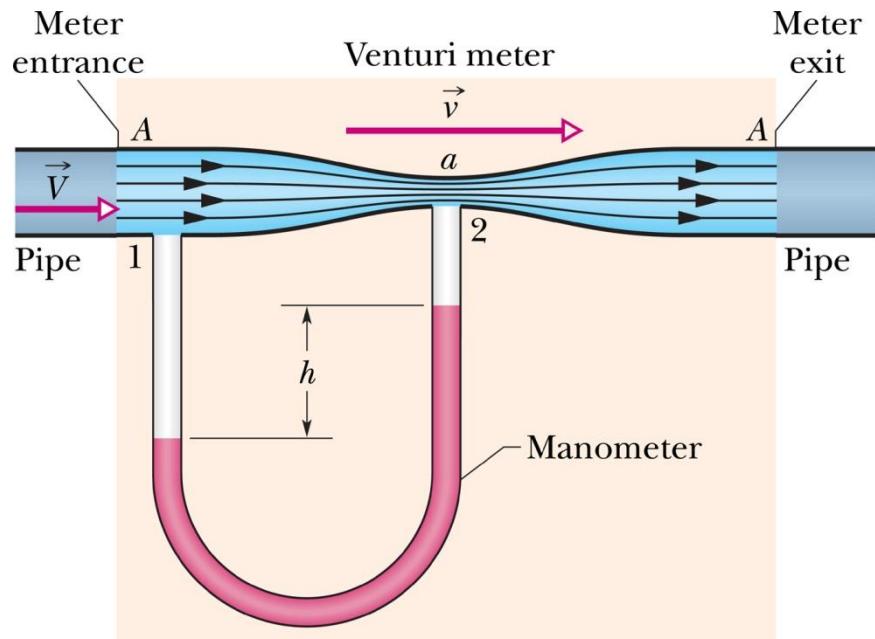


$$av = Av_0 \longrightarrow v_0 = \frac{a}{A}v$$
$$(a \ll A \rightarrow v_0 \ll v)$$

$$p_0 + \frac{1}{2}\rho v_0^2 + \rho gh = p_0 + \frac{1}{2}\rho v^2$$

$$v = \sqrt{2gh}$$

Venturi tube



$$v_A = \sqrt{\frac{2a^2 \Delta p}{\rho(A^2 - a^2)}}$$

$$AV = av$$

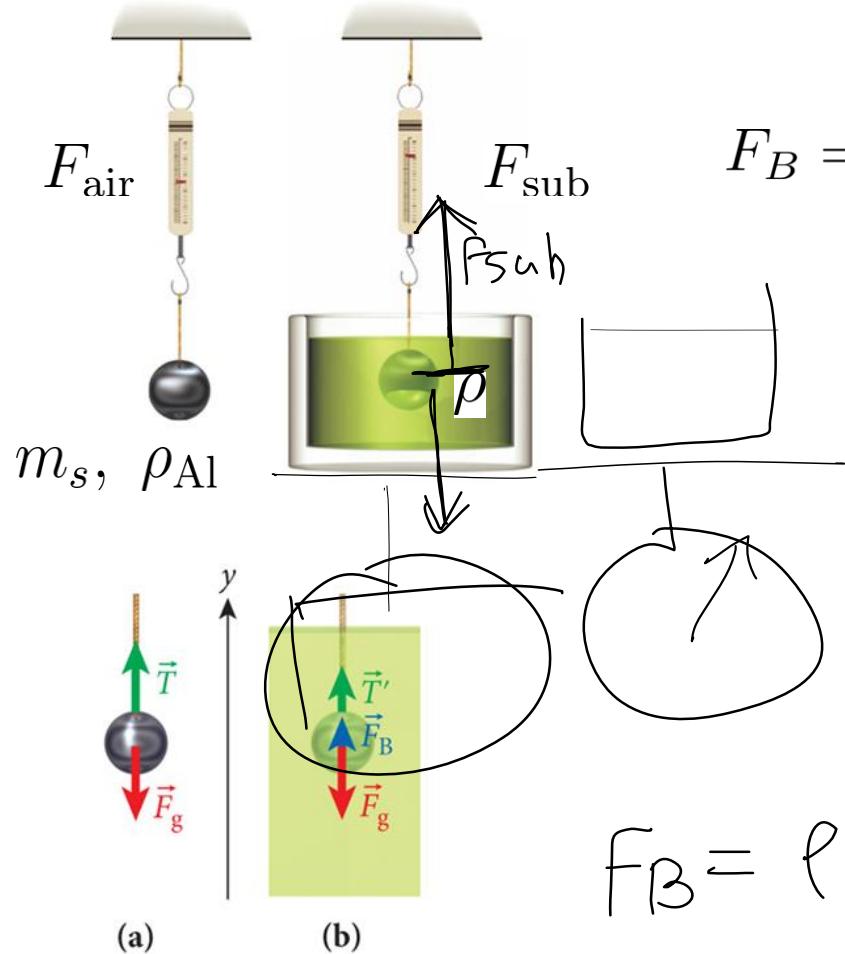
$$\Delta P = P_1 - P_2$$

$$P_1 + \frac{1}{2} \rho V^2 = P_2 + \frac{1}{2} \rho v^2 = P_2 + \frac{1}{2} \rho \left(\frac{A}{a}\right)^2 v^2$$

$$\frac{1}{2} \rho V^2 \left[\frac{A^2}{a^2} - 1 \right] = \Delta P$$

$$V^2 = \frac{2\Delta P}{\rho} \frac{a^2}{\frac{A^2}{a^2} - 1}$$

SP 13.3 Density of unknown liquid



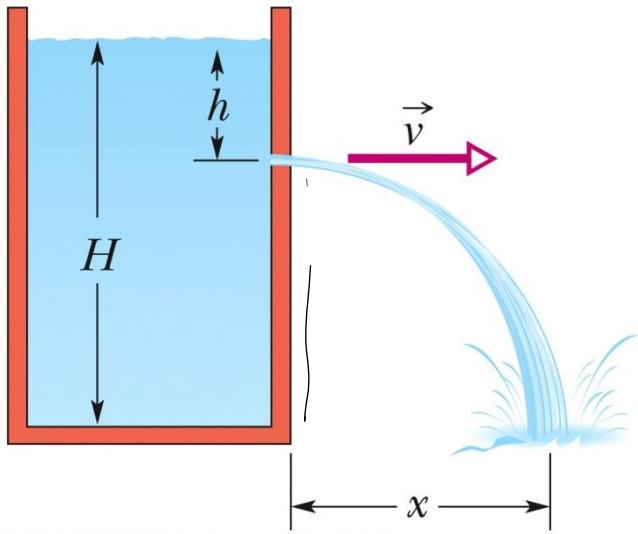
$$F_B = F_{\text{air}} - F_{\text{sub}} = mg = \rho V g$$

$$V = \frac{m_s}{\rho_{\text{Al}}} = \frac{F_{\text{air}}}{\rho_{\text{Al}} g}$$

$$\rho = \rho_{\text{Al}} \frac{F_{\text{air}} - F_{\text{sub}}}{F_{\text{air}}}$$

$$F_B = \cancel{\rho g} \frac{F_{\text{air}}}{\cancel{\rho_{\text{Al}} g}} \Rightarrow \rho = \rho_{\text{Al}} \frac{F_{\text{air}} - F_{\text{sub}}}{F_{\text{air}}}$$

Problem 1



h for given x
Maximum x

$$v = \sqrt{2gh}$$

$$h^2 - ht + \frac{x^2}{4} = 0$$

$$h = \frac{1}{2} \left(t \pm \sqrt{t^2 - x^2} \right)$$

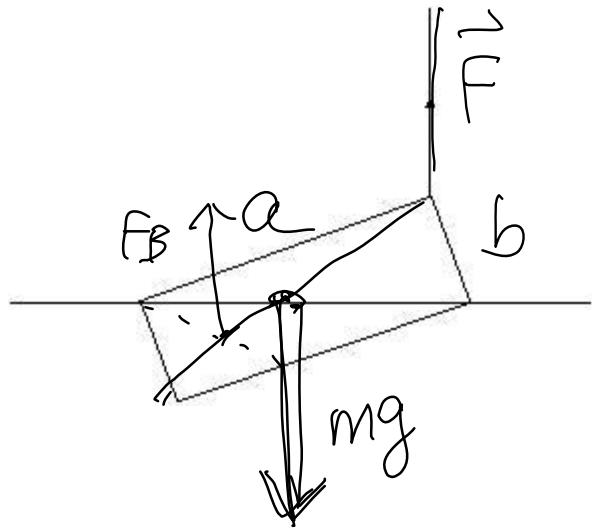
$$H - h = \frac{1}{2} g t^2$$

$$t = \sqrt{\frac{2(H-h)}{g}} \quad \sqrt{\frac{2g}{h}} \sqrt{\frac{2(H-h)}{g}} = X$$

$$X = 2 \sqrt{h(H-h)} \quad \frac{x^2}{4} = h - 1 - h^2$$

$$hH - h^2 = -(h^2 - hH) = -\left(h - \frac{H}{2}\right)^2 + \frac{H^2}{4}$$

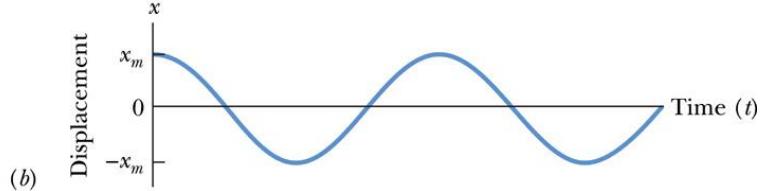
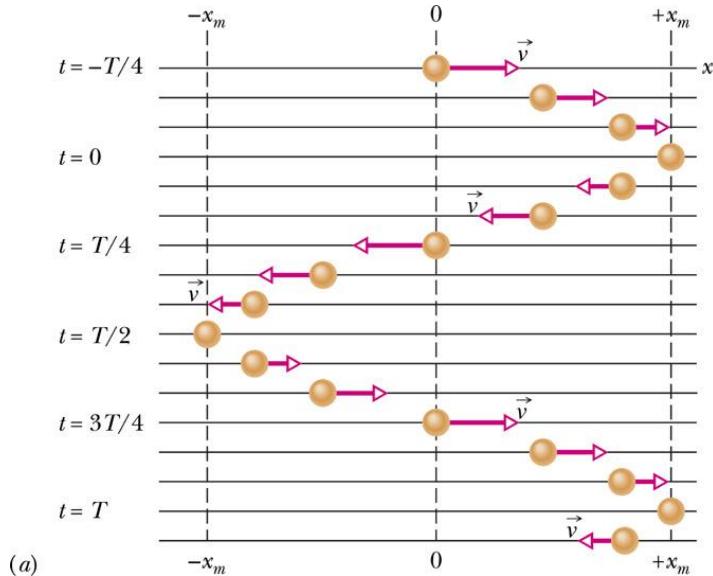
Problem 2



Ch. 14. Oscillations



Simple harmonic motion



periodic motion, harmonic motion

frequency: 1 hertz = 1 Hz = 초당 1회 진동 = 1 s^{-1}

$$\text{period } T \quad T = \frac{1}{f}$$

Displacement at time t

$$x(t) = x_m \cos(\omega t + \phi)$$

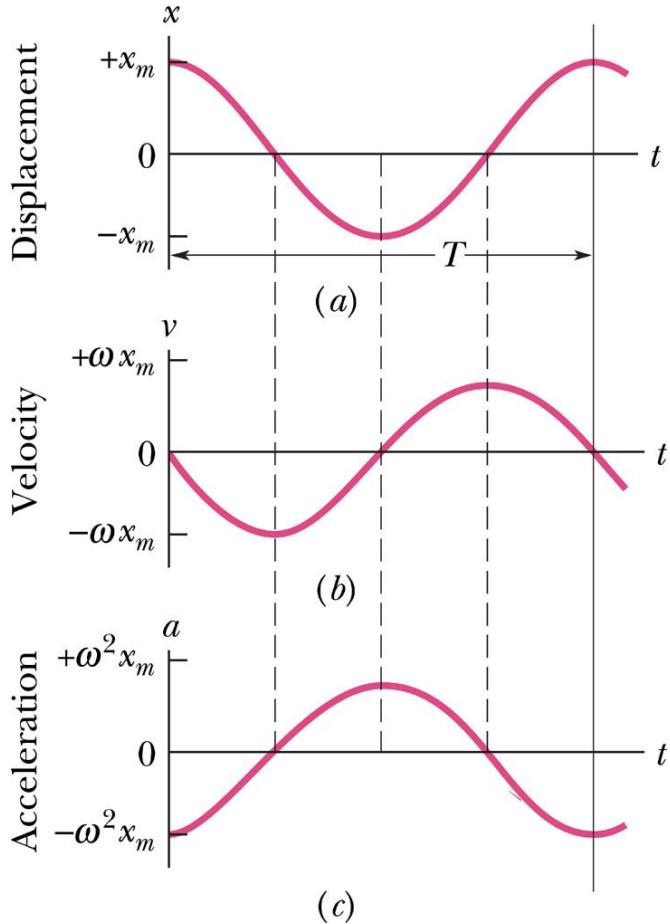
Diagram illustrating the components of the displacement equation:

- Amplitude: x_m
- Angular frequency: ω
- Time: t
- Phase constant or phase angle: ϕ
- Phase: $\omega t + \phi$

Mathematical derivation:

$$x_m \cos \omega t = x_m \cos \omega(t + T)$$
$$\omega(t + T) = \omega t + 2\pi$$
$$\omega T = 2\pi$$
$$\omega = \frac{2\pi}{T} = 2\pi f$$

SHO의 속도, 가속도



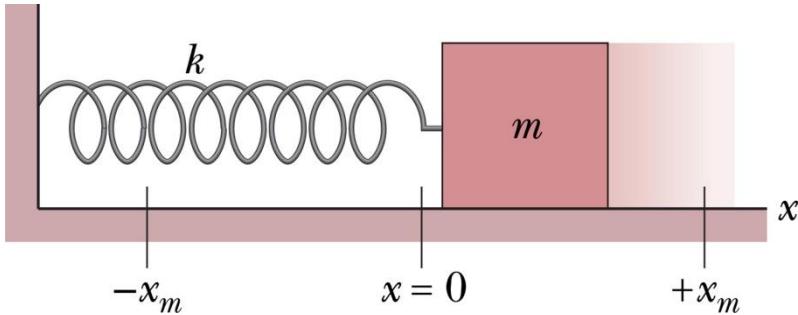
$$x(t) = x_m \cos(\omega t + \phi)$$

$$v(t) = \frac{dx}{dt} = -\omega x_m \sin(\omega t + \phi)$$

$$a(t) = \frac{dv}{dt} = -\omega^2 x_m \cos(\omega t + \phi)$$

$$a(t) = -\omega^2 x(t)$$

Simple harmonic motion

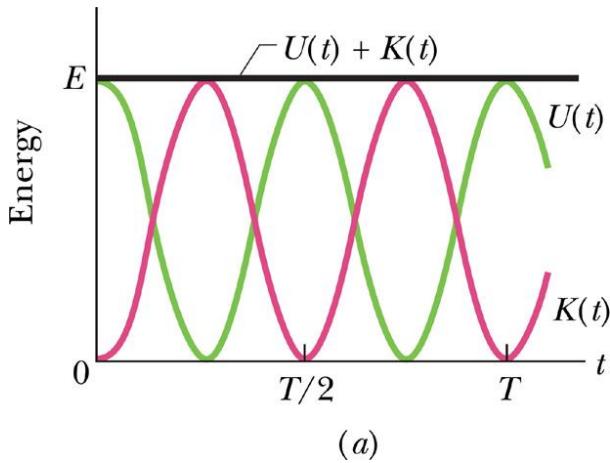


$$F = ma = -m\omega^2 x = -kx$$

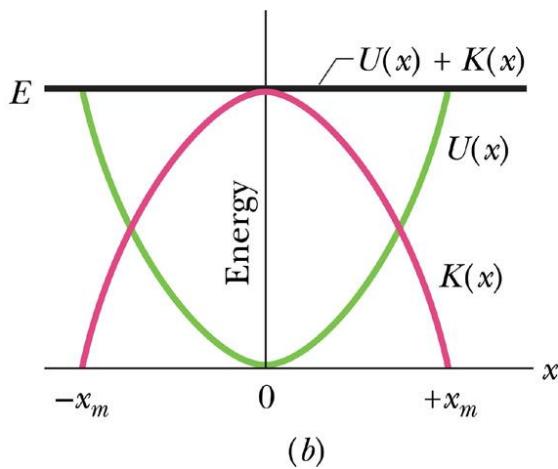
$$k = m\omega^2$$

Angular frequency $\omega = \sqrt{\frac{k}{m}}$ period $T = 2\pi\sqrt{\frac{m}{k}}$

Simple harmonic motion의 에너지



(a)



(b)

퍼텐셜에너지

$$U(t) = \frac{1}{2}kx^2 = \frac{1}{2}kx_m^2 \cos^2(\omega t + \phi)$$

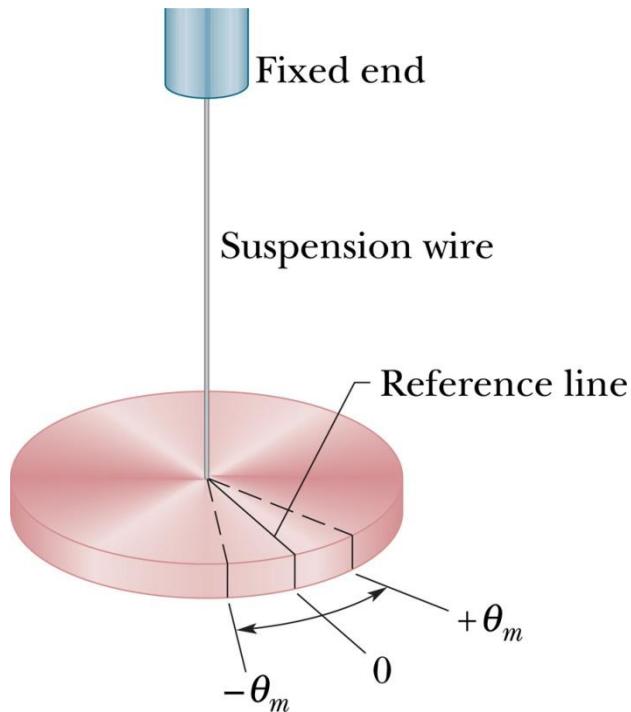
운동에너지

$$K(t) = \frac{1}{2}mv^2 = \frac{1}{2}m\omega^2x_m^2 \sin^2(\omega t + \phi)$$

역학적 에너지

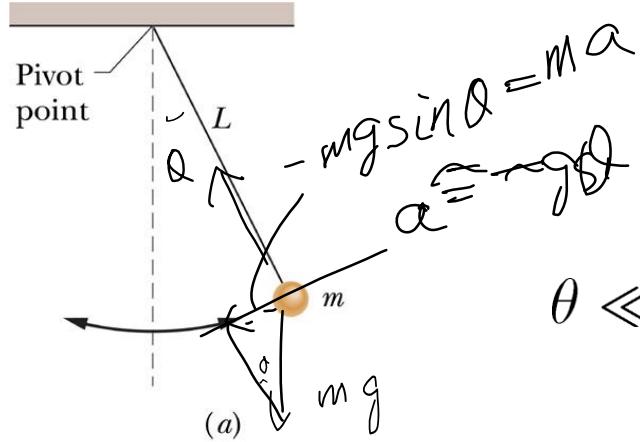
$$E = U(t) + K(t) = \frac{1}{2}kx_m^2$$

Angular simple harmonic oscillator



$$\tau = -\kappa\theta \quad T = 2\pi\sqrt{\frac{I}{\kappa}}$$

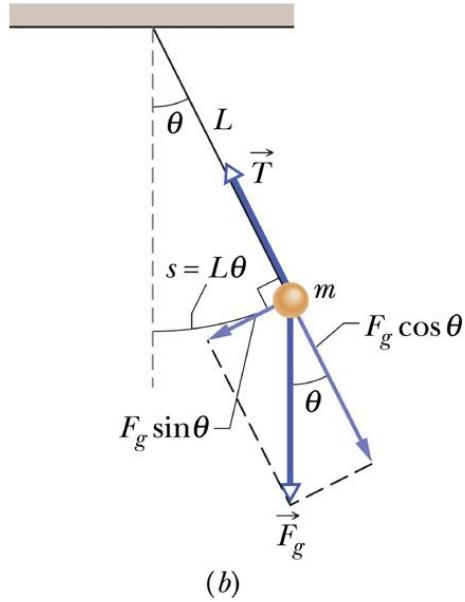
Pendulum



$$\tau = -L(F_g \sin \theta) = I\alpha$$

$\theta \ll 1$ 일 때

$$\alpha = \frac{mgL}{I}\theta$$

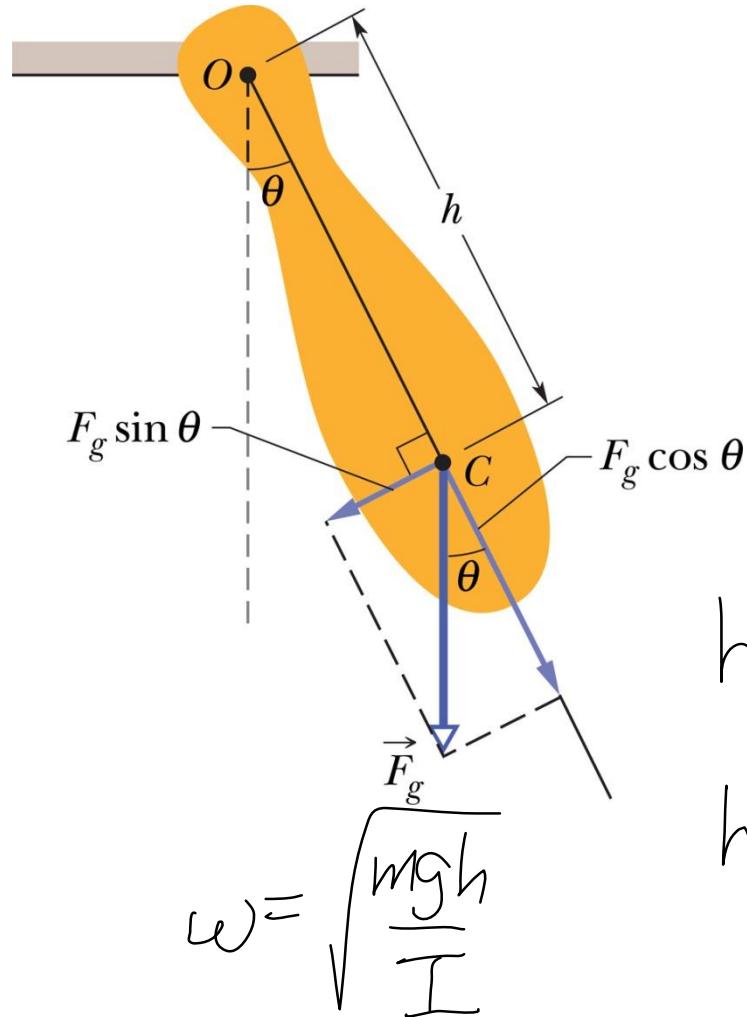


$$\omega = \sqrt{mgL/I} \quad I = mL^2$$

$$\omega = \sqrt{\frac{g}{L}}$$

$$T = 2\pi \sqrt{\frac{I}{mgL}} = 2\pi \sqrt{\frac{L}{g}}$$

Physical pendulum



$$T = 2\pi \sqrt{\frac{I}{mgh}}$$

$$\frac{I}{mgh} = \frac{L_0}{g} \rightarrow L_0 = \frac{I}{mh}$$

$$hF_g \sin \theta = I \alpha \quad \omega^2$$

$$hF_g \theta \quad \text{ss}$$

$$\alpha = \left(\frac{mgh}{I} \right) \theta$$