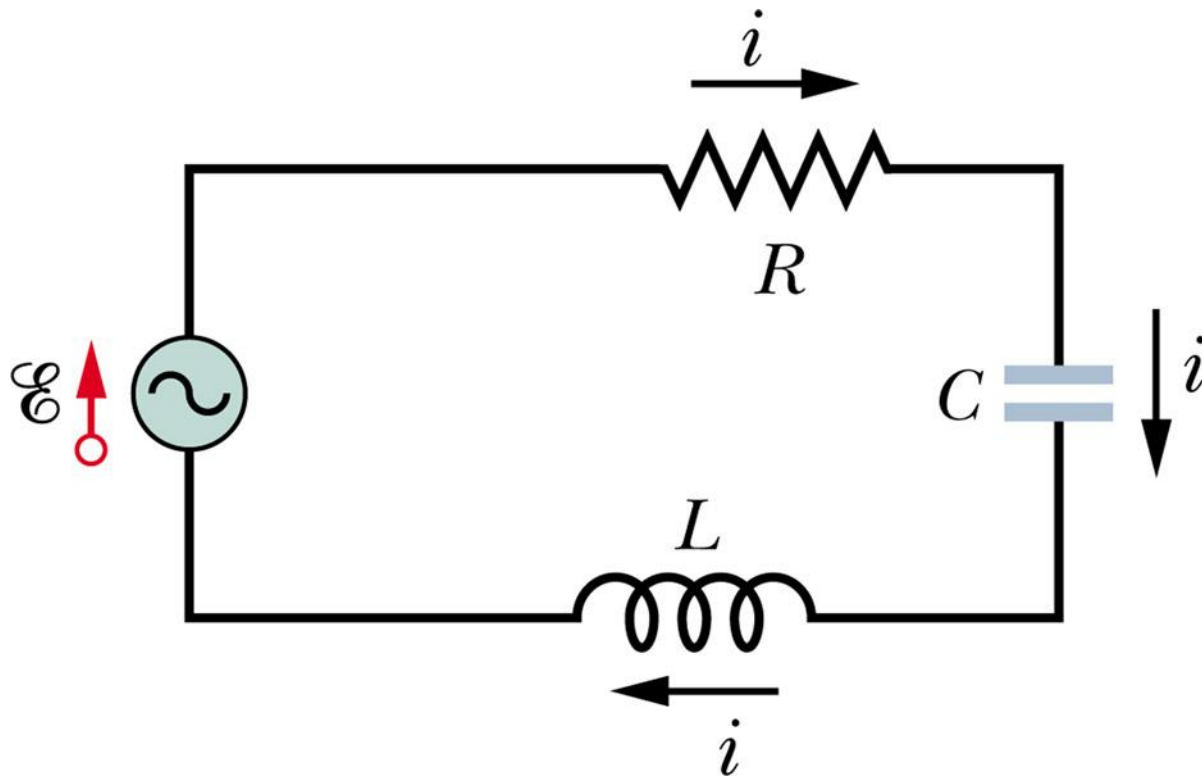


Copyright statement

- The images and the pictures in this lecture are provided by the CDs accompanied by the books
 1. University Physics, Bauer and Westfall, McGraw-Hill, 2011.
 2. Principles of Physics, Halliday, Resnick, and Walker, Wiley, 8th and 9th Ed.
- The rest is made by me.

RLC circuits

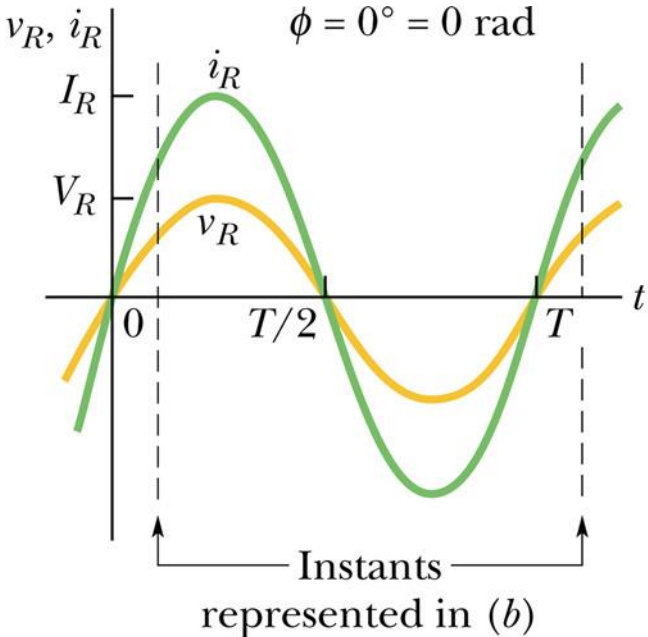


$$\mathcal{E} = \mathcal{E}_m \sin \omega_d t$$

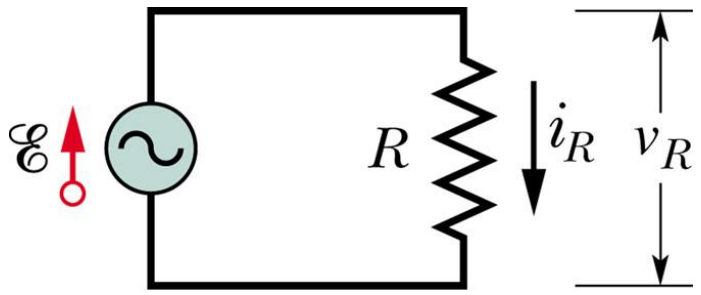
$$i = I \sin(\omega_d t - \phi)$$

I 와 ϕ 구하기

Circuit with R



(a)

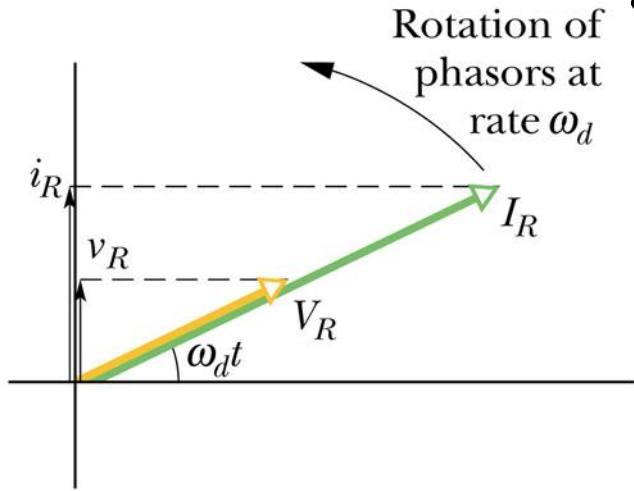


$$\mathcal{E} - v_R = 0 \longrightarrow v_R = \mathcal{E}_m \sin \omega_d t = V_R \sin \omega_d t$$

$$i_R = \frac{v_R}{R} = \frac{V_R}{R} \sin \omega_d t \longrightarrow \phi = 0$$

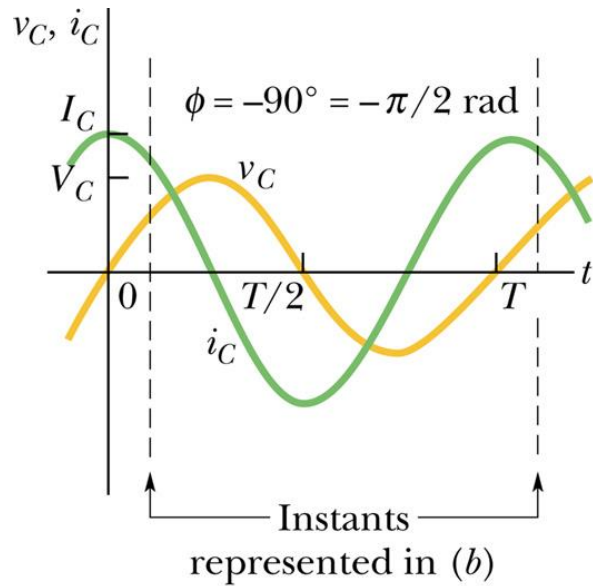
$$i_R = I_R \sin(\omega_d t - \phi)$$

$$V_R = I_R R$$

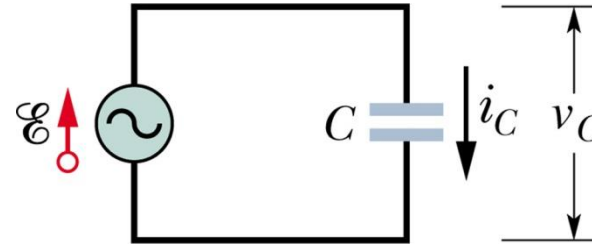


(b)

Circuit with C



(a)



$$v_C = V_C \sin \omega_d t$$

$$q_C = C v_C = C V_C \sin \omega_d t$$

$$i_C = \frac{dq_C}{dt} = \omega_d C V_C \cos \omega_d t$$

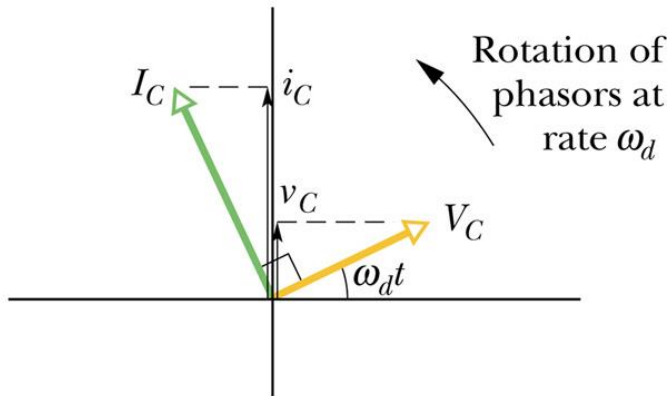
축전기형 저항 (capacitive resistance)

$$X_C = \frac{1}{\omega_d C}$$

$$\cos \omega_d t = \sin(\omega_d t + 90^\circ)$$

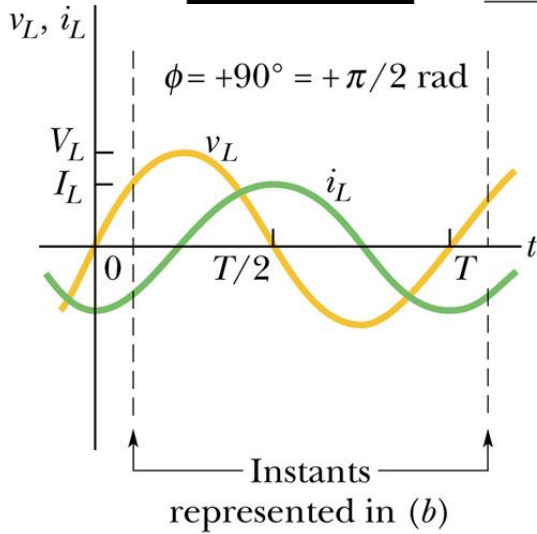
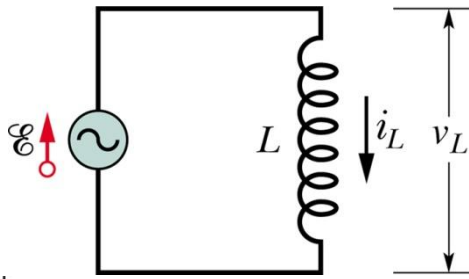
$$i_C = \frac{V_C}{X_C} \sin(\omega_d t + 90^\circ) = I_C \sin(\omega_d t - \phi) \longrightarrow \phi = -\frac{\pi}{2}$$

$$V_C = I_C X_C$$



(b)

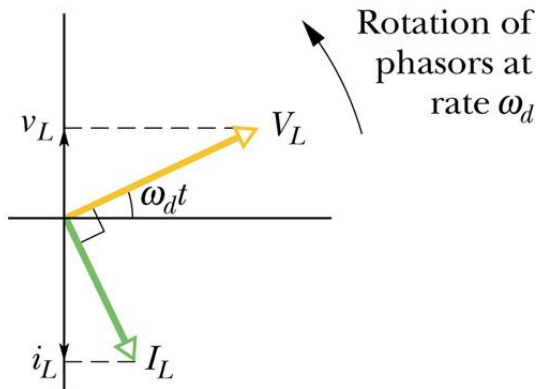
Circuit with L



(a)

유도형 저항 (inductive resistance)

$$X_L = \omega_d L$$



(b)

$$v_L = V_L \sin \omega_d t = L \frac{di_L}{dt}$$

$$i_L = \int di_L = \frac{V_L}{L} \int \sin \omega_d t dt = -\frac{V_L}{\omega_d L} \cos \omega_d t$$

$$-\cos \omega_d t = \sin(\omega_d t - 90^\circ)$$

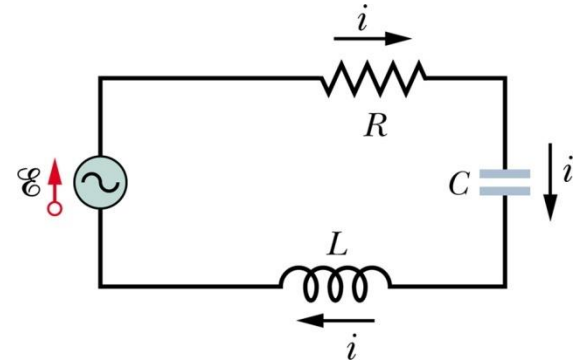
$$i_L = \frac{V_L}{X_L} \sin(\omega_d t - 90^\circ) = I_L \sin(\omega_d t - \phi) \longrightarrow \phi = \frac{\pi}{2}$$

$$V_L = I_L X_L$$

RLC 회로

$$\begin{aligned}\mathcal{E} &= \mathcal{E}_m \sin \omega_d t, \\ i &= I \sin(\omega_d t - \phi).\end{aligned}$$

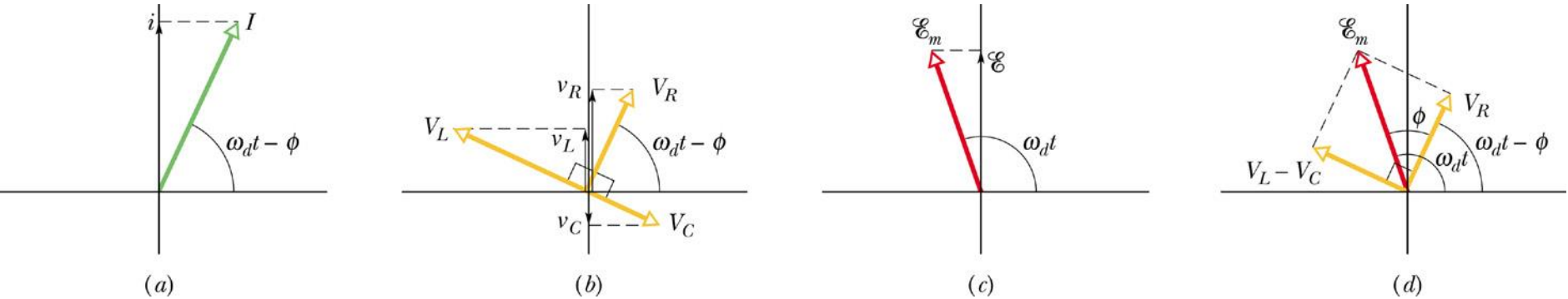
- 저항: 전류는 퍼텐셜과 같은 위상.
- 축전기: 전류가 90도 빠름.
- 인덕터: 전류가 90도 느림.



$$\mathcal{E}_m^2 = V_R^2 + (V_L - V_C)^2 = (IR)^2 + (IX_L - IX_C)^2$$

$$\begin{aligned}I &= \frac{\mathcal{E}_m}{\sqrt{R^2 + (X_L - X_C)^2}} = \frac{\mathcal{E}_m}{Z} \\ &= \frac{\mathcal{E}_m}{\sqrt{R^2 + (\omega_d L - 1/(\omega_d C))^2}}\end{aligned}$$

Series RLC circuit



$$\mathcal{E} = \mathcal{E}_m \sin \omega_d t, \quad i = I \sin(\omega_d t - \phi)$$

$$\mathcal{E} = v_R + v_C + v_L$$

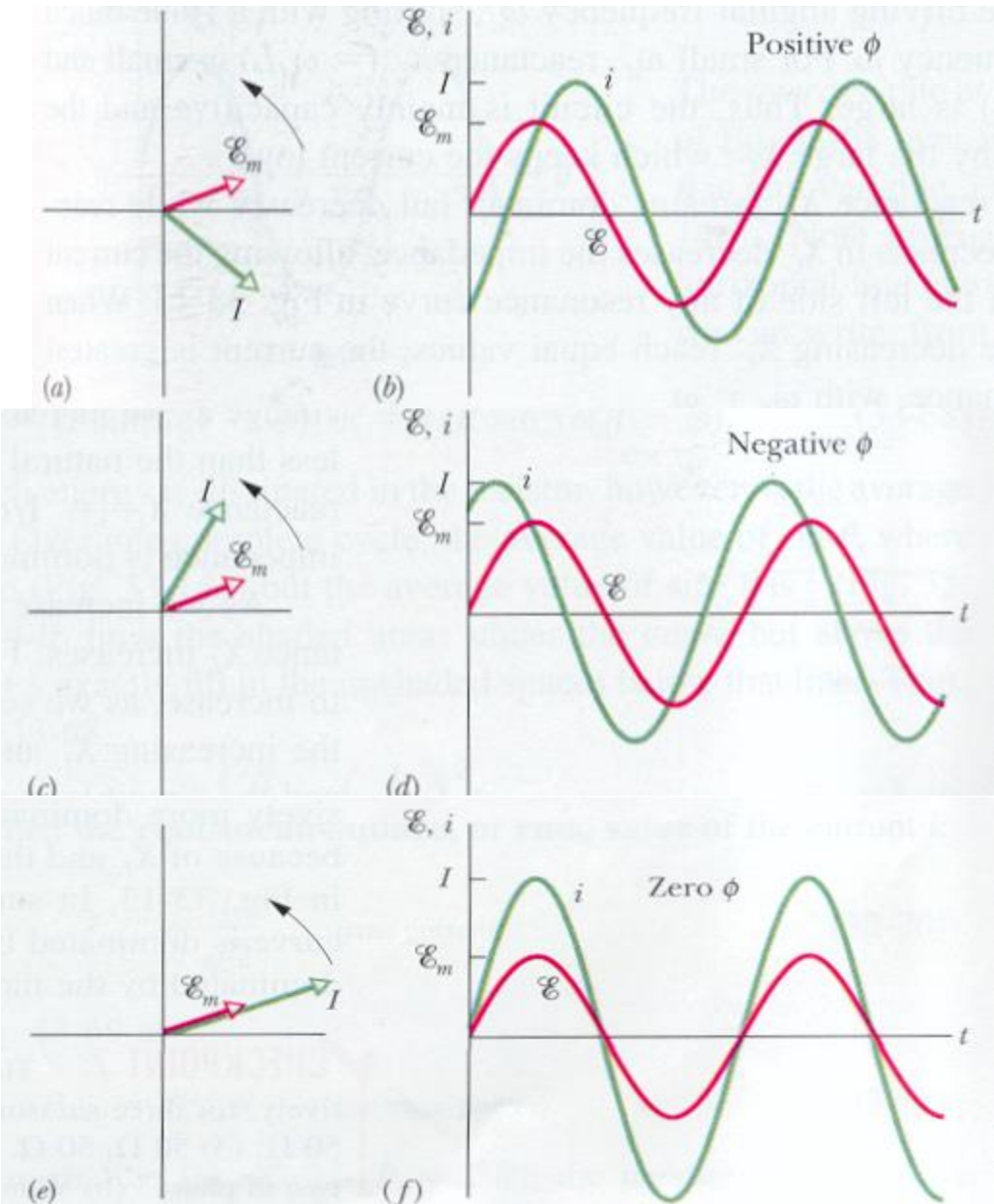
$$\mathcal{E}_m^2 = V_R^2 + (V_L - V_C)^2 = (IR)^2 + (IX_L - IX_C)^2$$

$$I = \frac{\mathcal{E}_m}{\sqrt{R^2 + (X_L - X_C)^2}} \quad \text{impedance} \quad Z = \sqrt{R^2 + (X_L - X_C)^2}$$

$$I = \frac{\mathcal{E}_m}{Z} = \frac{\mathcal{E}_m}{\sqrt{R^2 + (\omega_d L - 1/\omega_d C)^2}}$$

$$\tan \phi = \frac{V_L - V_C}{V_R} = \frac{X_L - X_C}{R}$$

Phase constants and resonance



$$X_L > X_C$$

$$X_L < X_C$$

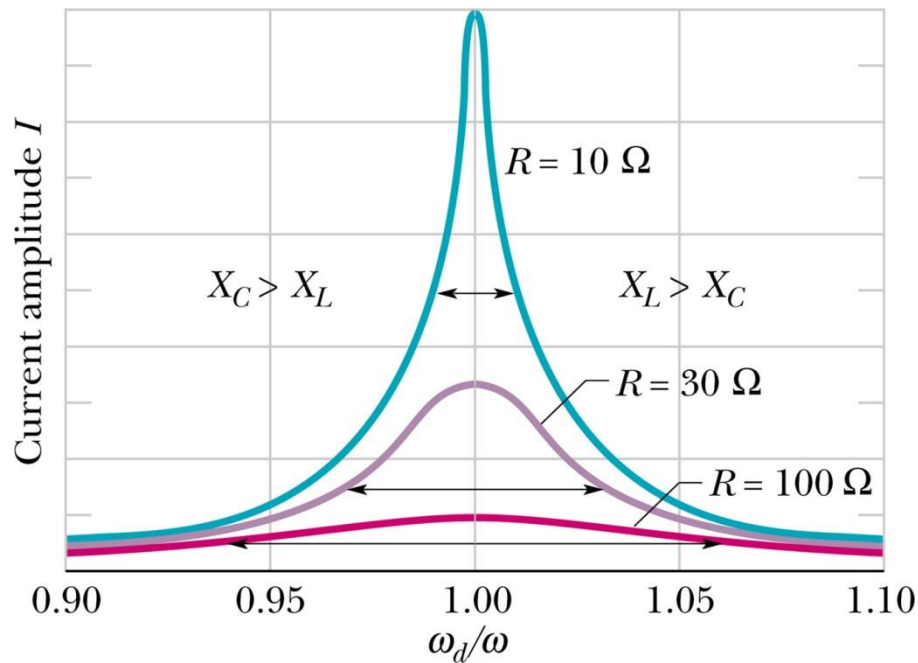
$$X_L = X_C$$

phase

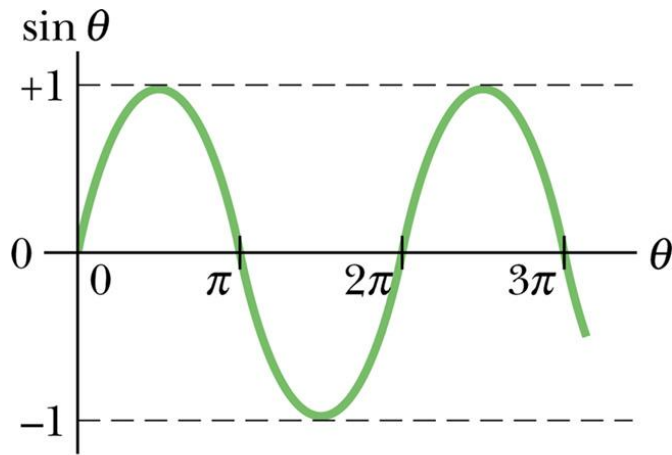
$$\tan \phi = \frac{V_L - V_C}{V_R} = \frac{IX_C - IX_L}{IR} = \frac{X_L - X_C}{R}.$$

공명현상 (resonance)
흐르는 전류가 최대일 조건

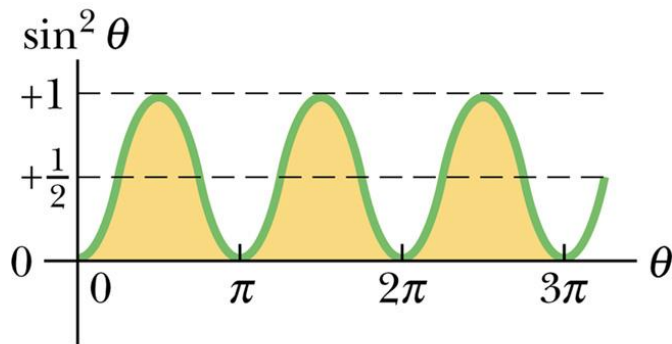
$$\omega_d = \omega = \frac{1}{\sqrt{LC}}$$



Power in AC circuits



(a)



(b)

$$P = i^2 R = I^2 R \sin^2(\omega_d t - \phi)$$

$$P_{\text{av}} = \frac{I^2 R}{2} = \left(\frac{I}{\sqrt{2}}\right)^2 R = I_{\text{rms}}^2 R$$

$$I_{\text{rms}} = \frac{I}{\sqrt{2}}, \quad V_{\text{rms}} = \frac{V}{\sqrt{2}}, \quad \mathcal{E}_{\text{rms}} = \frac{\mathcal{E}_m}{\sqrt{2}}$$

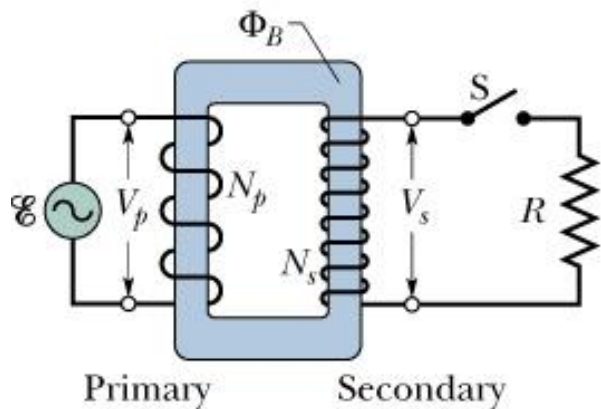
$$I_{\text{rms}} = \frac{\mathcal{E}_{\text{rms}}}{\sqrt{2}} = \frac{\mathcal{E}_{\text{rms}}}{\sqrt{R^2 + (X_L - X_C)^2}}$$

$$P_{\text{av}} = \frac{\mathcal{E}_{\text{rms}}}{Z} I_{\text{rms}} \frac{R}{Z}$$

$$\cos \phi = \frac{V_R}{\mathcal{E}_m} = \frac{IR}{IZ} = \frac{R}{Z}$$

$$P_{\text{av}} = \mathcal{E}_{\text{rms}} I_{\text{rms}} \cos \phi$$

Transformer



$$\mathcal{E} = \mathcal{E}_m \sin \omega t$$

$$\mathcal{E}_{\text{turn}} = \frac{d\phi_B}{dt}$$

$$V_p = N_P \mathcal{E}_{\text{turn}}$$

$$V_s = N_s \mathcal{E}_{\text{turn}}$$

$$\mathcal{E}_{\text{turn}} = \frac{V_p}{N_p} = \frac{V_s}{N_s}$$

$$V_s = V_p \frac{N_s}{N_p}$$

회로에 연결된 경우

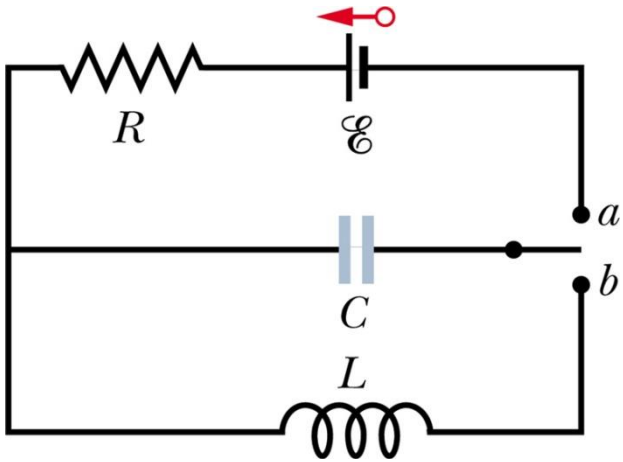
$$I_p V_p = I_s V_s$$

$$I_s = I_p \frac{N_p}{N_s} = \frac{V_s}{R} = V_p \frac{N_s}{N_p} \frac{1}{R}$$

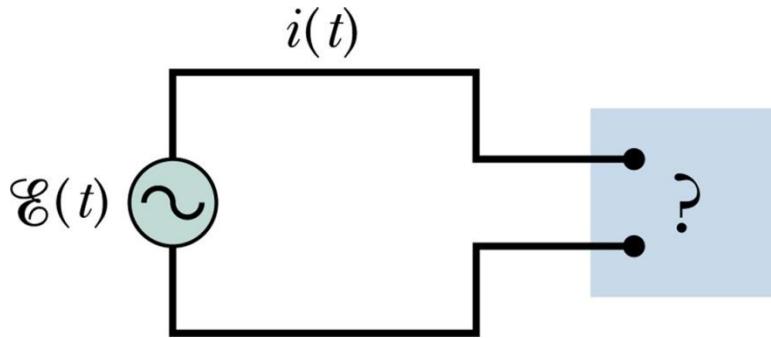
$$I_p = \frac{1}{R} \left(\frac{N_s}{N_p} \right)^2 V_p$$

$$R_{\text{eq}} = \left(\frac{N_p}{N_s} \right)^2 R$$

Problem



Problem



$$\mathcal{E}(t) = (75.0\text{V}) \sin \omega_d t$$

$$i(t) = (1.20\text{A}) \sin(\omega_d t + 42.0^\circ)$$

- (a) Power factor?
- (b) Current leading or lagging the emf?
- (c) Inductive or capacitive?
- (d) In resonance?
- (e) Capacitor? Or an inductor? Or a resistor?
- (f) Average energy transfer

Chap. 31 Electromagnetic waves



Laws on E&M so far

Electric
field

$$\oint \vec{E} \cdot d\vec{A} = \frac{q}{\epsilon_0}$$

Gauss' law on static charges
(equivalent to Coulomb's law)

$$\oint \vec{E} \cdot d\vec{s} = -\frac{d\Phi_B}{dt}$$

Faraday's law
Induced electric field due to
time-varying magnetic field

Magnetic
field

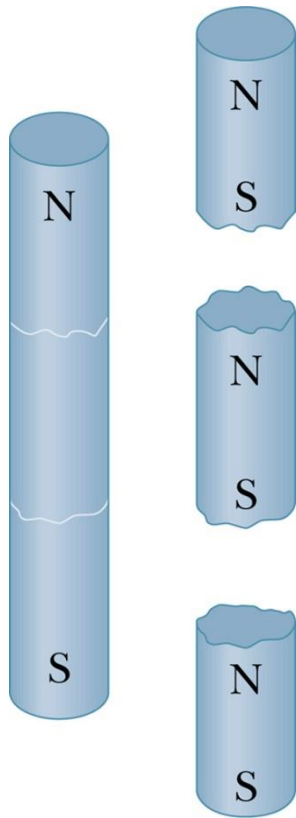
$$\oint \vec{B} \cdot d\vec{A} = 0$$

Gauss' law on magnetic field
No magnetic charges

$$\oint \vec{B} \cdot d\vec{s} = \mu_0 i$$

Ampere's law
Magnetic field produced by
a current

Gauss' law on magnetic field



Magnetic fields are always produced by **magnetic dipoles**.

Magnetic flux $\Phi_B = \oint \vec{B} \cdot d\vec{A} = 0$

n.b.: $\Phi_E = \oint \vec{E} \cdot d\vec{A} = \frac{q_{\text{enc}}}{\epsilon_0}$

Induced magnetic field

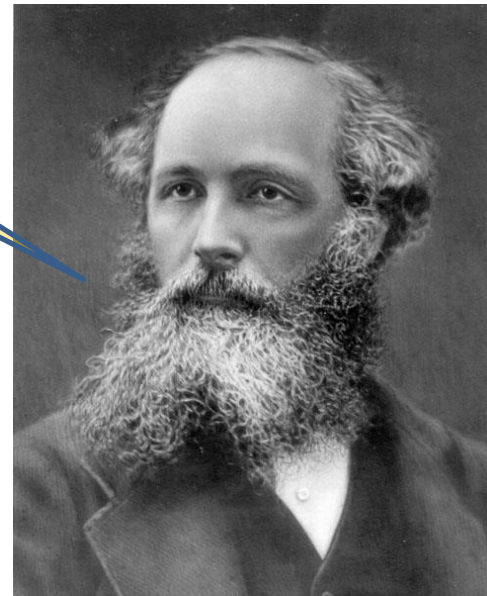
Faraday's law:
$$\oint \vec{E} \cdot d\vec{s} = -\frac{d\Phi_B}{dt}$$

On the other hand, can a time-varying electric field induce a magnetic field?

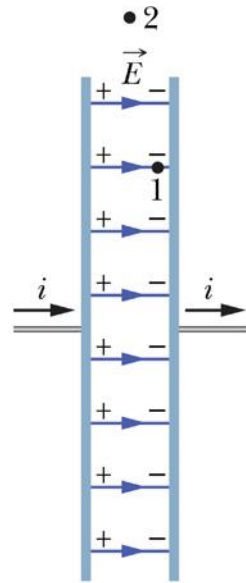
$$\oint \vec{B} \cdot d\vec{s} = \mu_0 \epsilon_0 \frac{d\Phi_E}{dt}$$

Maxwell's induction law

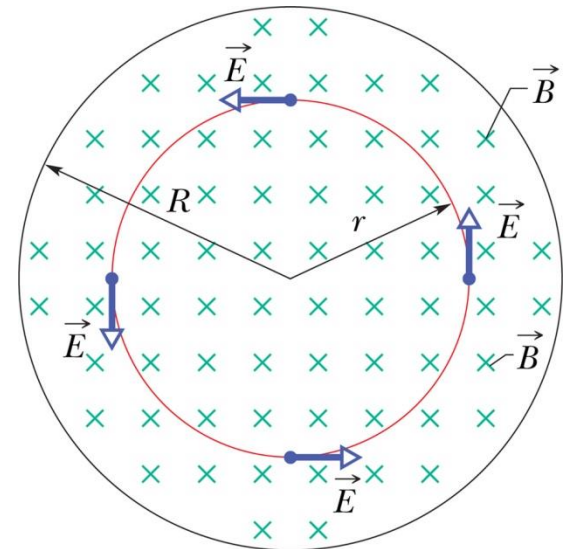
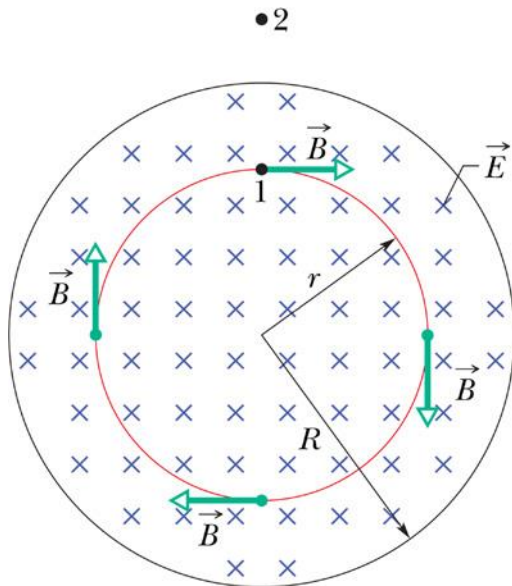
Yes!



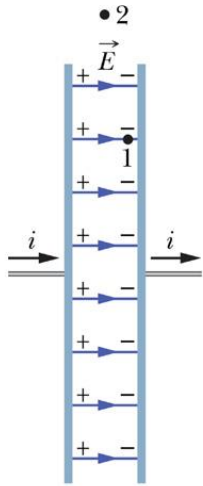
Ampere-Maxwell's law



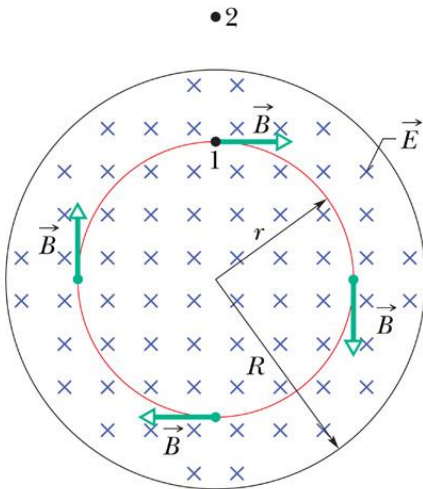
$$\oint \vec{B} \cdot d\vec{s} = \mu_0 \epsilon_0 \frac{d\Phi_E}{dt} + \mu_0 i_{\text{enc}}$$



Example



(a)

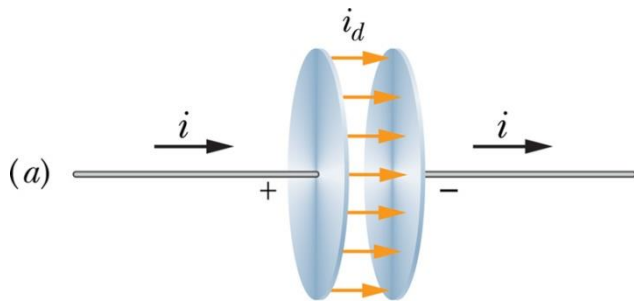


(b)

displacement current

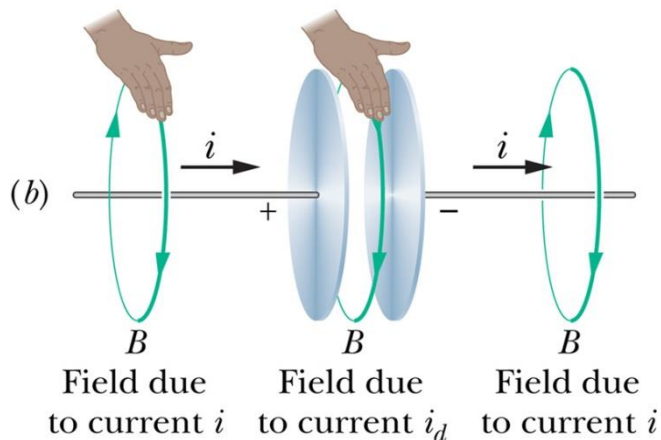
$$i_d = \epsilon_0 \frac{d\Phi_E}{dt}$$

$$\oint \vec{B} \cdot d\vec{s} = \mu_0 i_{d,enc} + \mu_0 i_{enc} \quad \text{Ampere-Maxwell's law}$$



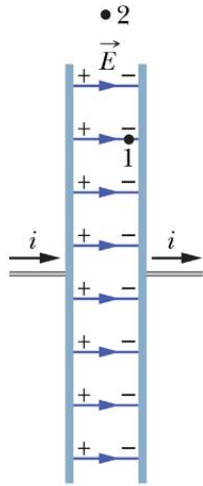
$$q = \epsilon_0 A E \quad \frac{dq}{dt} = i = \epsilon_0 A \frac{dE}{dt}$$

$$i_d = \epsilon_0 \frac{d\Phi_E}{dt} = \epsilon_0 \frac{d(EA)}{dt} = \epsilon_0 A \frac{dE}{dt}$$

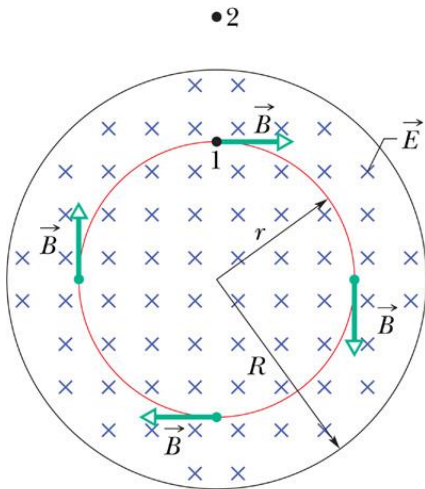


$$B = \begin{cases} i_d = i \\ \left(\frac{\mu_0 i_d}{2\pi R^2} \right) r, & \text{Inside C} \\ \frac{\mu_0 i_d}{2\pi r} & \text{Outside C} \end{cases}$$

Sample



(a)



(b)

Maxwell's equations

Maxwell's Equations^a

Name	Equation	
Gauss' law for electricity	$\oint \vec{E} \cdot d\vec{A} = q_{\text{enc}}/\epsilon_0$	Relates net electric flux to net enclosed electric charge
Gauss' law for magnetism	$\oint \vec{B} \cdot d\vec{A} = 0$	Relates net magnetic flux to net enclosed magnetic charge
Faraday's law	$\oint \vec{E} \cdot d\vec{s} = -\frac{d\Phi_B}{dt}$	Relates induced electric field to changing magnetic flux
Ampere–Maxwell law	$\oint \vec{B} \cdot d\vec{s} = \mu_0\epsilon_0 \frac{d\Phi_E}{dt} + \mu_0 i_{\text{enc}}$	Relates induced magnetic field to changing electric flux and to current

^aWritten on the assumption that no dielectric or magnetic materials are present.