

LECTURE 6

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6. Basic Opamp Design and Compensation

6.3 Advanced Current Mirrors

6.4 Folded-Cascode Opamp

6.5 Current Mirror Opamp

6.6 Linear Settling Time Revisited

6.7 Fully Differential Folded-Cascode Opamp

6.8 Common-Mode Feedback Circuits



Gain Boosting

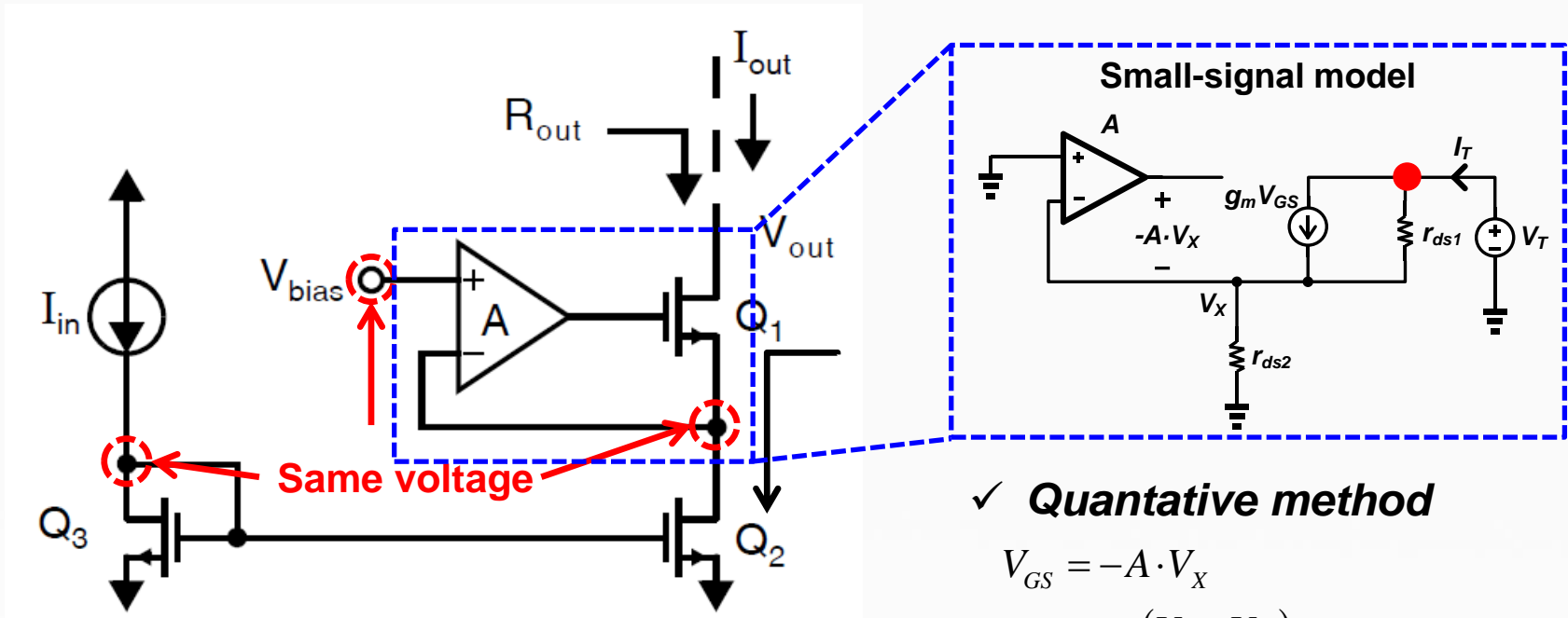


Fig. 6.13 The enhanced output-impedance current mirror.

- ✓ **Intuitive method**
- Keep the V_{DS2}
- **Increase the output impedance**

✓ **Quantative method**

$$V_{GS} = -A \cdot V_X$$

KCL :
$$g_m V_{GS} + \frac{(V_T - V_X)}{r_{ds1}} = I_T$$

$$V_X = I_T \cdot r_{ds2}$$



$$R_{out} = \frac{V_T}{I_T} = (A+1)g_m r_{ds2} r_{ds1} + r_{ds2} r_{ds1}$$

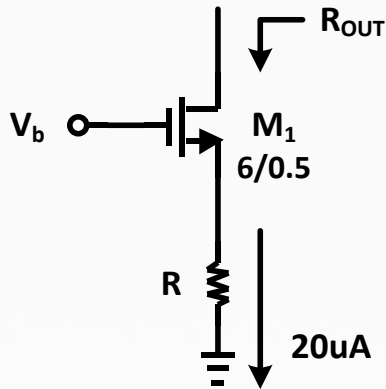
$$R_{out} \cong g_m r_{ds1} r_{ds2} (1+A)$$



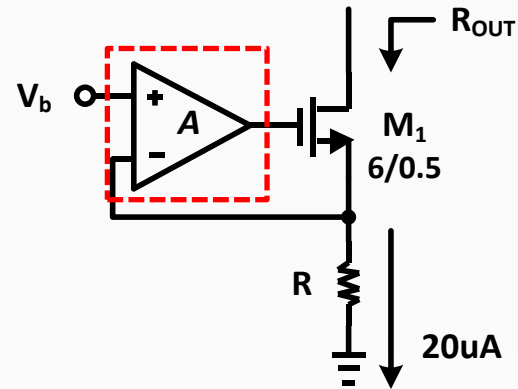
Example

두 회로의 **Output Impedance**를 비교하라.

$$R = 10k\Omega, \mu_n C_{OX} = 270\mu A/V^2, I_D = 20\mu A, \lambda = 0.1, A = 100$$



(a) NMOS with source resistance



(b) Gain boosting applied

$$g_{m1} = \sqrt{\mu_n C_{OX} (W/L) 2I_D}$$

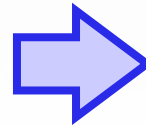
$$= 2.54 \times 10^{-4} S$$

$$r_{o1} = \frac{1}{\lambda I_D} = 500k\Omega$$

$$R_{OUT} = g_{m1} r_{o1} R + r_{o1} + R$$

$$= g_{m1} r_{o1} R$$

$$= 1.27M\Omega$$



$$R_{OUT} = (A + 1) g_{m1} r_{o1} R + r_{o1} R$$

$$= A g_{m1} r_{o1} R$$

$$= 127M\Omega$$



Output impedance increased 100 times



Enhanced Output-Impedance Current Mirror

- Bedrich J, Hosticka, Swiss Federal Institute of Technology (1979년)

- Current mirror using gain boosting technique

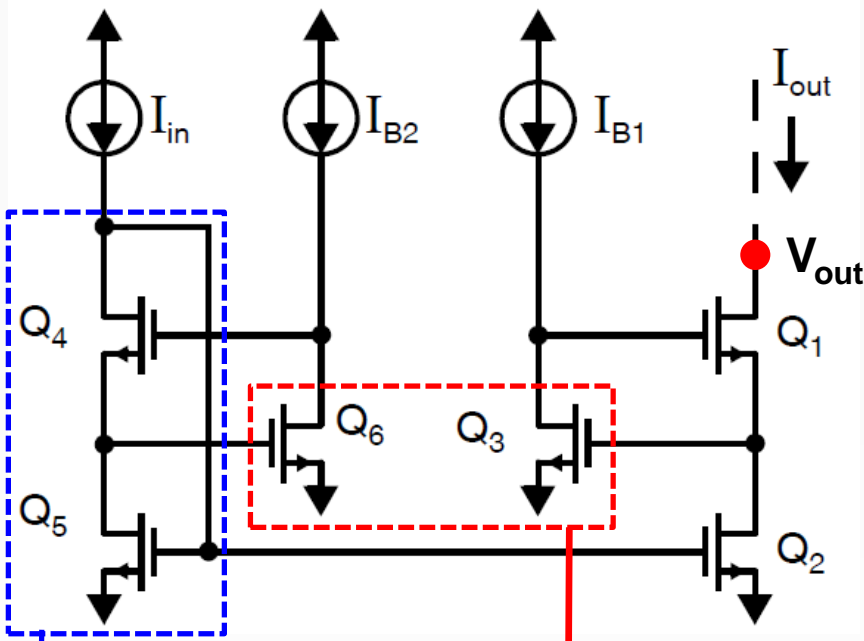


Fig. 6.15 The Sackinger implementation of the enhanced output-impedance current mirror.

Wide-range current mirror

Gain boosting

$$I_{in} = I_{out}$$

$$R_{out} \cong \frac{g_{m1} g_{m3} r_{ds1} r_{ds2} r_{ds3}}{2}$$

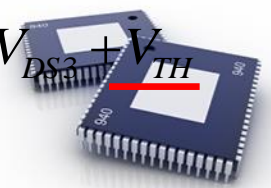
😊 High output impedance
Equal current

😞 Output swing limited by Q₃

$$V_{out} > V_{DS1} + V_{DS2}$$

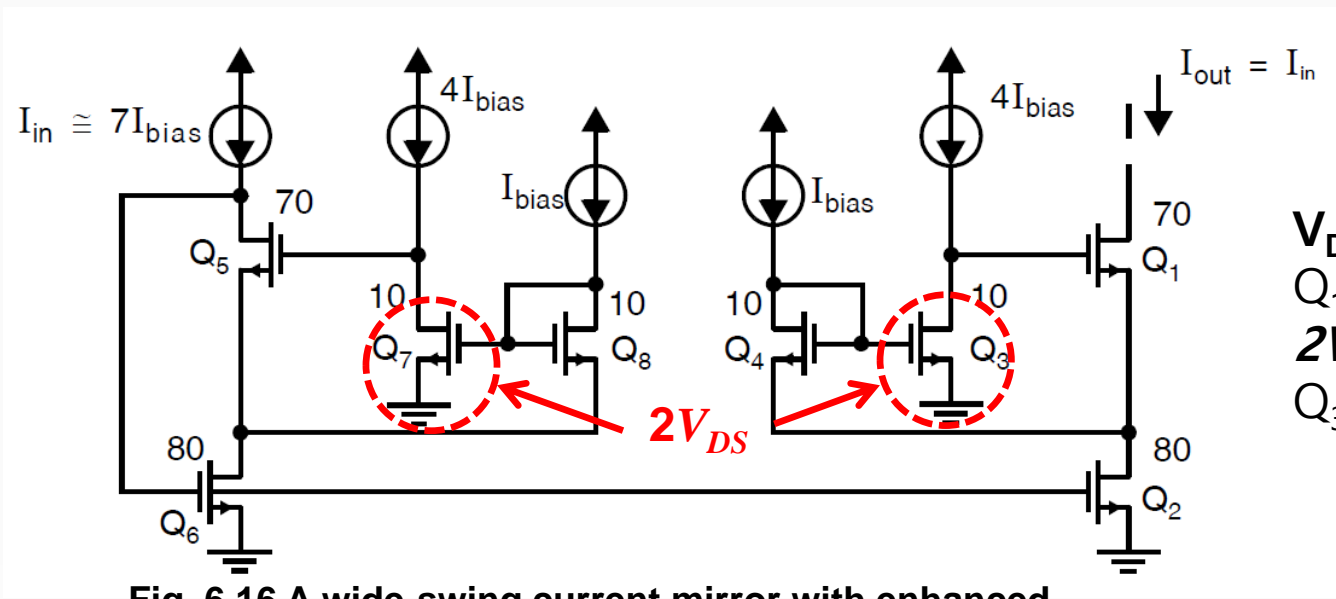


$$V_{out} > V_{DS1} + V_{GS3} = V_{DS1} + V_{DS3} + V_{TH}$$



Wide-Swing Current Mirror

- Umberto Gatti, University of Pavia (1990년)



$$V_{DS} (= V_{GS} - V_{TH} = V_{eff})$$

Q₁, Q₂, Q₄, Q₅, Q₆, Q₈

$$2V_{DS}$$

Q₃, Q₇

Fig. 6.16 A wide-swing current mirror with enhanced output impedance..

$$V_{G3} = V_{DS2} + V_{GS4} = 2 \cdot V_{DS} + V_{TH}$$

$$V_{DS2} = V_{S4} = V_{G3} - V_{GS4}$$

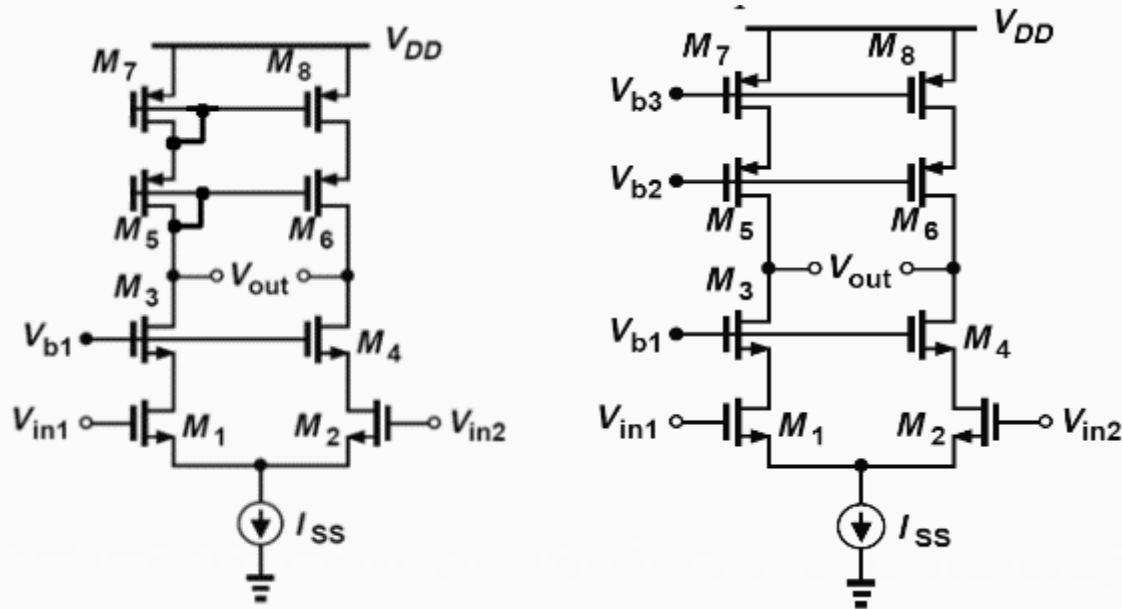
$$= (2V_{DS} + V_{TH}) - (V_{DS} + V_{TH}) = V_{DS}$$

$$V_{out} > V_{DS2} + V_{DS1} = \underline{2V_{DS}}$$

- 😊 High output impedance
- 😊 Equal current
- 😊 Wide-Swing
- 😞 Power dissipation(x2)
- 😞 Additional poles



Folded Cascode Op amp



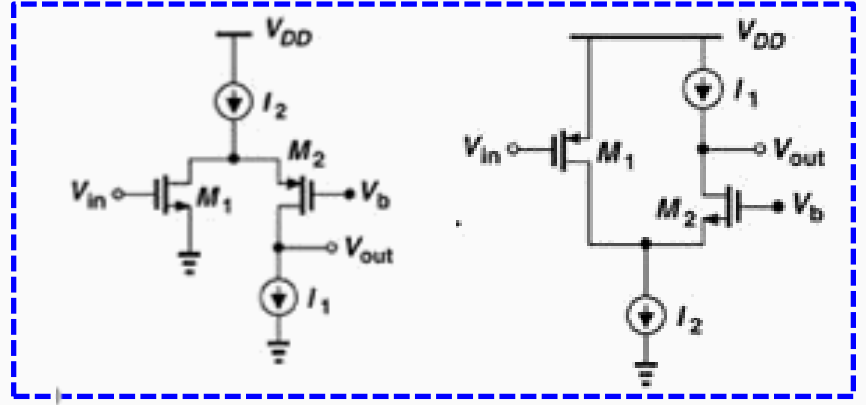
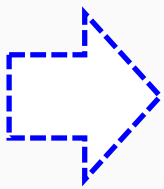
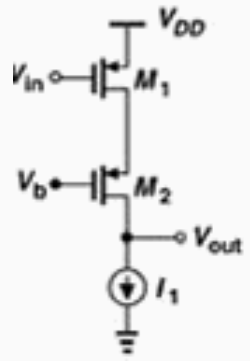
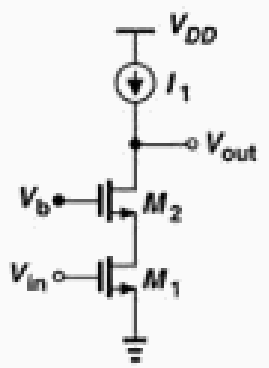
😊 **High gain**

$$|A_v| \approx g_{m1,2} (g_{m4} r_{ds4} r_{ds2} \parallel g_{m6} r_{ds6} r_{ds8})$$

😞 **Output Swing**



Folded Cascode Op amp



Cascode circuits

Folded cascode circuits

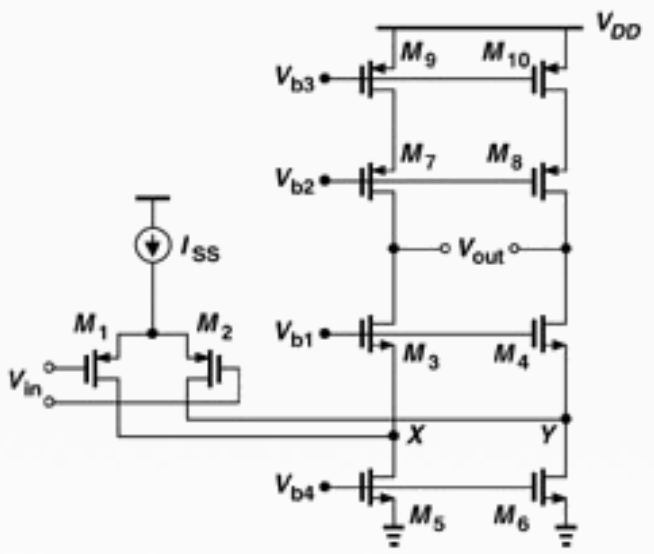
	Cascode	Folded Cascode
Swing	$V_{in} - V_{th} + V_{DS} \leq V_{out} \leq V_{DD} - V_{I1}$	$V_{I2} + V_{DS} \leq V_{out} \leq V_{DD} - V_{I1}$
Power	$P = V_{DD} \cdot I_1$	$P = V_{DD} \cdot I_2 = V_{DD} \cdot 2I_1$

😊 **V_{out} is independent of V_{in}.(Swing)**

😞 **Power dissipation**



Folded Cascode Op amp



$$|A_v| \approx g_{m1} \left[g_{m3} r_{o3} (r_{o1} \parallel r_{o5}) \parallel g_{m7} r_{o7} r_{o9} \right]$$

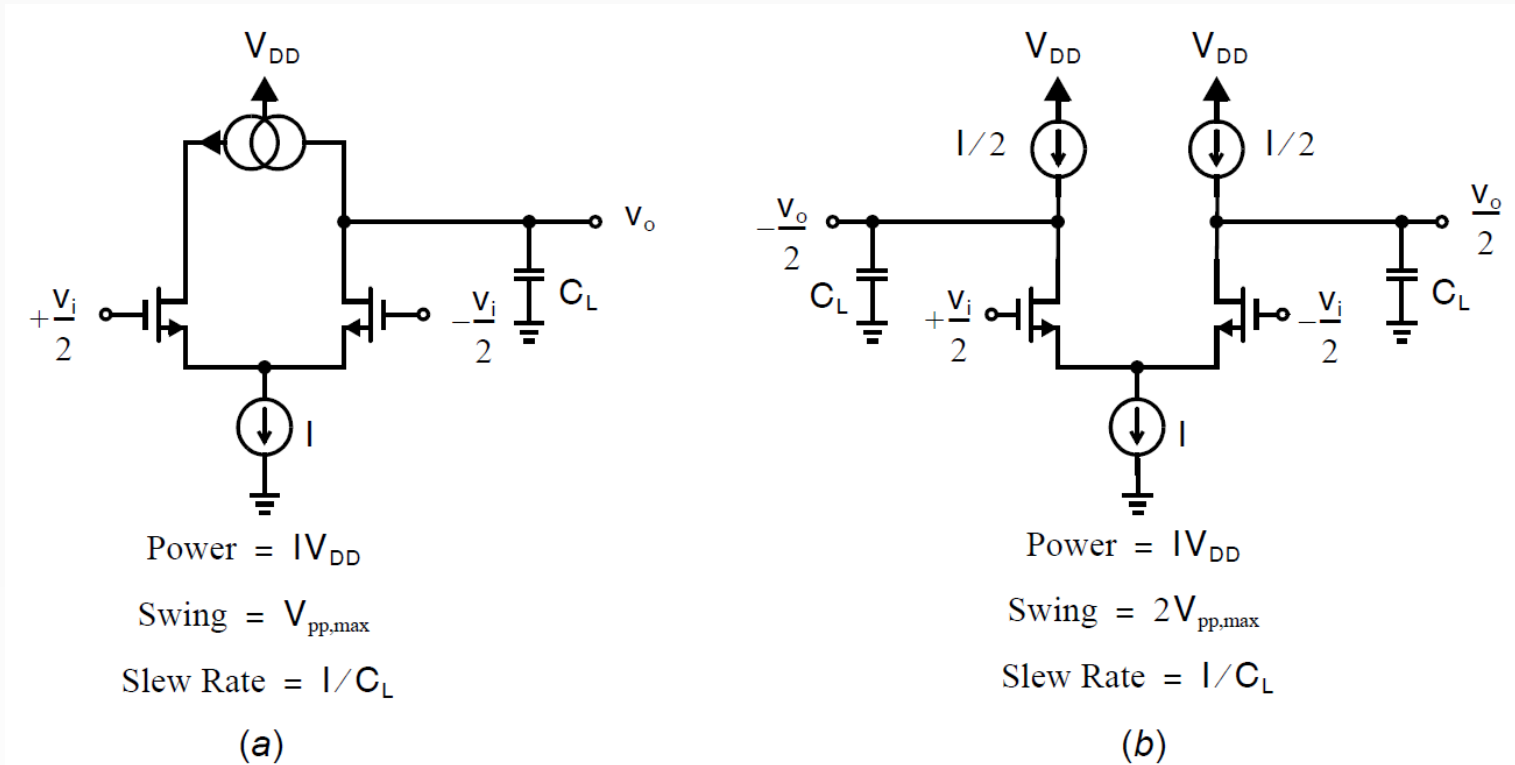
$$P_{\text{dominant}} \approx \frac{1}{C_L \cdot \left[g_{m3} r_{o3} (r_{o1} \parallel r_{o5}) \parallel g_{m7} r_{o7} r_{o9} \right]}$$

Fig. Folded-cascode op amp topology

- 😊 **Single pole, High speed, Good phase margin**
- 😞 **Power dissipation**

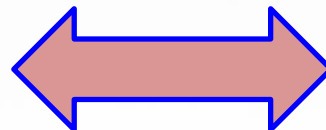


Single & Differential



Same

Power
 Slew-rate
 Gain



Advantage of Fully differential opamp

1. Twice the available swing
2. Canceling unwanted common-mode noise

Different

Swing(x2)



Example

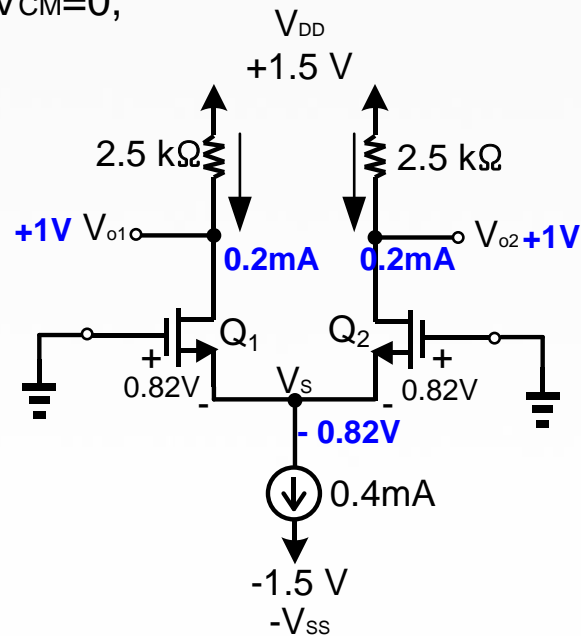
$V_{DD}=V_{SS}=1.5V$, $V_{GS}=0.82V$, $V_t=0.5V$, $I=0.4mA$, $R_D=2.5K\Omega$, Current source minimum voltage(V_{CS})= $0.4V$.

(a) For $V_{CM}=0$, find V_S and V_{out1} and V_{out2} .

(b) Repeat (a) for $V_{CM}= +1V$

(c) Repeat (a) for $V_{CM}= -0.2V$

(a) For $V_{CM}=0$,



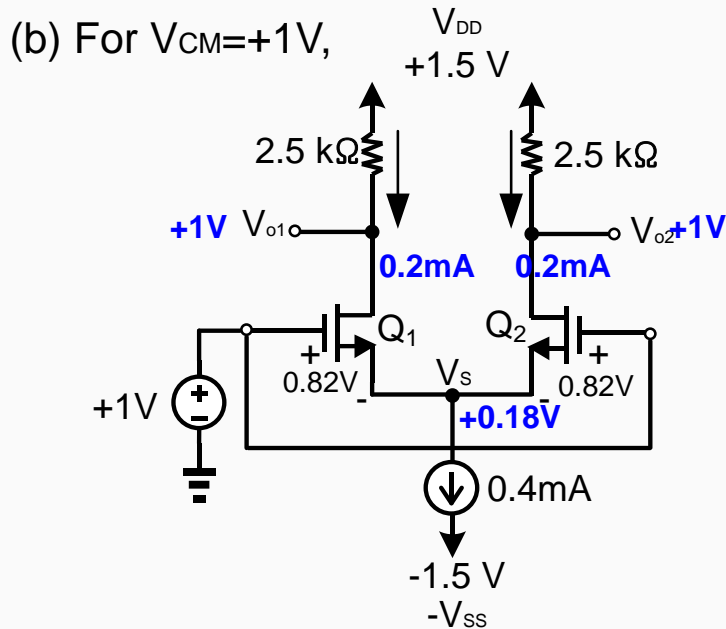
$$V_S = V_{CM} - V_{GS} = 0 - 0.82V = -0.82V$$

$$V_{O1} = V_{O2} = V_{DD} - \frac{1}{2} I_D$$

$$= 1.5 - 0.2 \times 2.5 = 1V$$



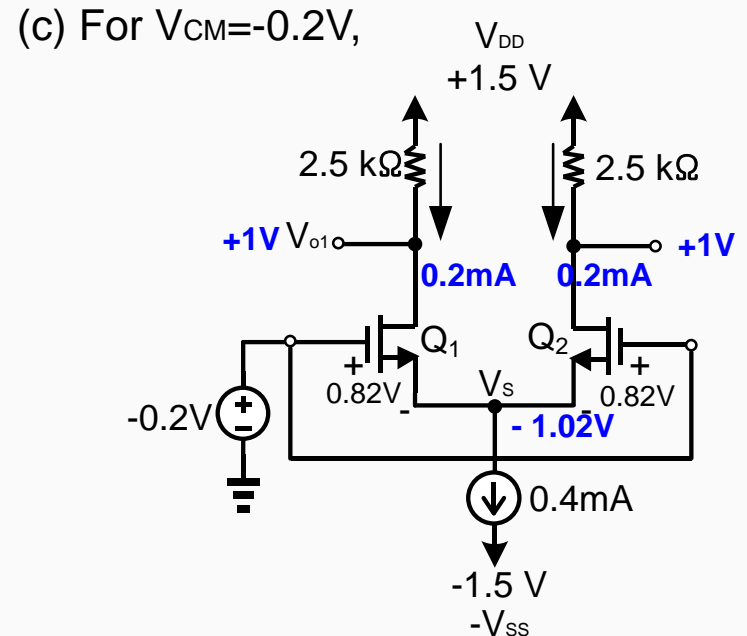
Example



$$V_S = V_{CM} - V_{GS} = 1 - 0.82V = +0.18V$$

$$V_{O1} = V_{O2} = V_{DD} - \frac{1}{2} I_D$$

$$= 1.5 - 0.2 \times 2.5 = 1V$$



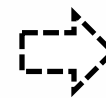
$$V_S = V_{CM} - V_{GS} = -0.2 - 0.82V = -1.02V$$

$$V_{CS} = -V_S - (-V_{SS}) = -1.02 + 1.5V = 0.48V \geq 0.4V$$

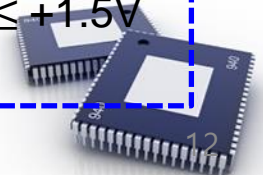
$$V_{O1} = V_{O2} = V_{DD} - \frac{1}{2} I_D = 1.5 - 0.2 \times 2.5 = 1V$$

$$V_{CM \max} = V_t + (V_{DD} - \frac{1}{2} I_D) = 0.5 + 1 = 1.5V$$

$$V_{CM \min} = -V_{SS} + V_{CS} + V_{GS} = -1.5 + 0.4 + 0.82 = -0.28V$$



$$-0.28V \leq V_{CM} \leq +1.5V$$



Common-mode Output voltage

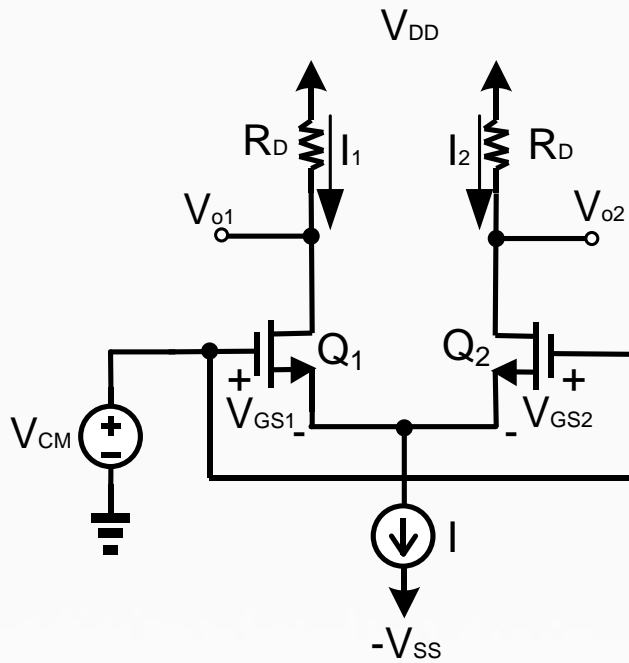
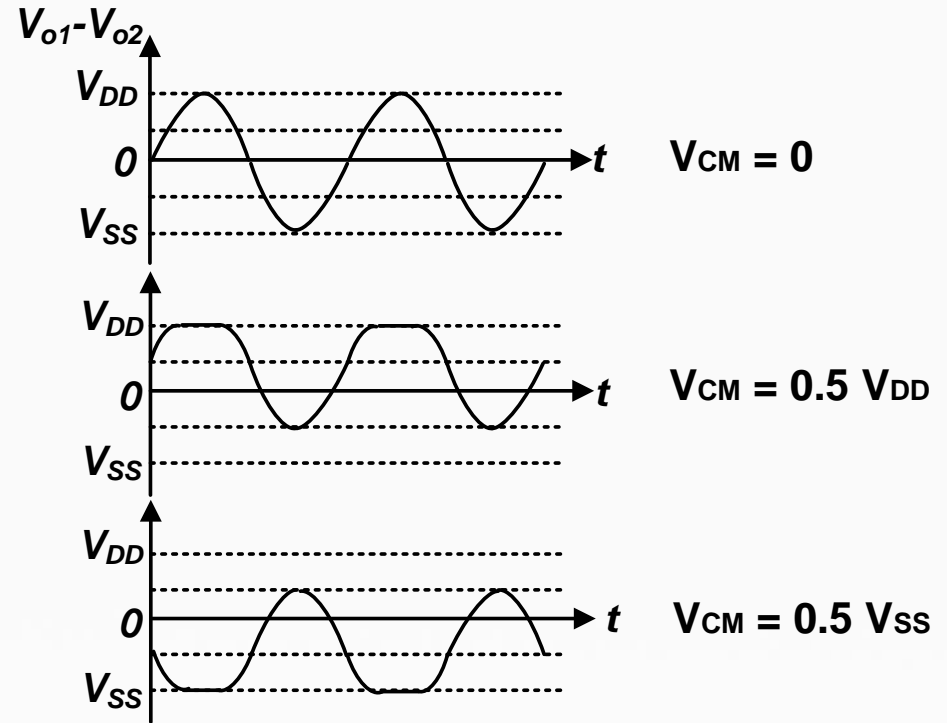


Fig. fully differential amp

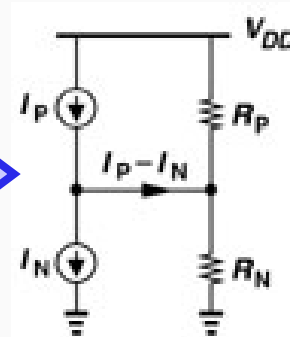
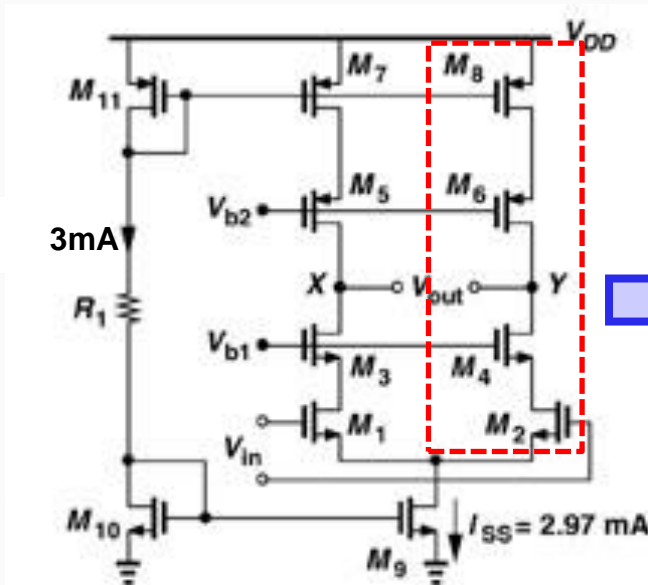


Influence of the output CM signal on differential amp

CM level is influenced by the mismatches and loads and can be at any value.



Why we need the CMFB?



Ideally $I_P = I_N$

In practice $I_P \neq I_N$ (mismatches)

$$(I_P - I_N)(R_P \parallel R_N) \rightarrow 0 \text{ or } V_{DD}$$

Depends on Quite high mismatches

Simplified model of high-gain amplifier

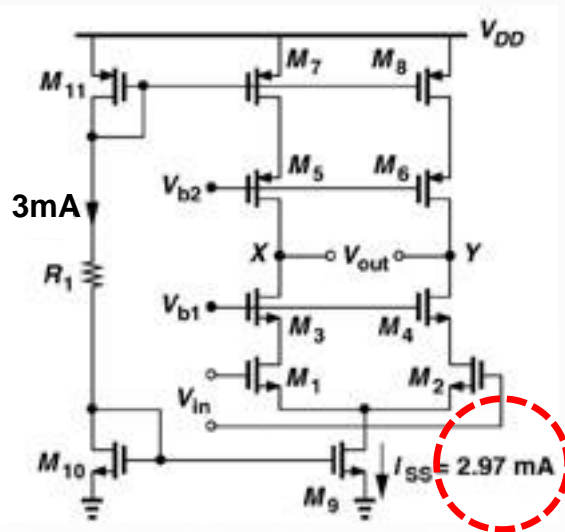
- 1) $I_{D5,6} > I_{SS}/2 \rightarrow$ both M_5 and $M_6 \rightarrow$ triode region
- 2) $I_{D3,4} < I_{SS}/2 \rightarrow$ both V_X and $V_Y \downarrow$, $M_5 \rightarrow$ triode region

☹️ **CM level poorly defined!!**



Example

Suppose M_9 suffers from a **1% current mismatch** with respect to M_{10} , producing $I_{SS}=2.97\text{mA}$ rather than 3mA .



Current mismatch

$$\text{Output impedance} \quad (g_{m6}r_{o6}r_{o8}) \parallel (g_{m4}r_{o4}r_{o2}) = 266\text{k}\Omega$$

$$\text{Current mismatch} \quad I_6 - I_4 = 15\mu\text{A}$$

$$\text{Output voltage error} \quad V_{err} = 266\text{k}\Omega \cdot 15\mu\text{A} = 3.99\text{V}$$

Too large to produce!

1. V_X and V_Y must rise
2. M_5 - M_6 and M_7 - M_8 enter the **triode region**
3. $I_{D7,8} = 1.485\text{mA}$.



CM level poorly defined!!



Concept of CMFB

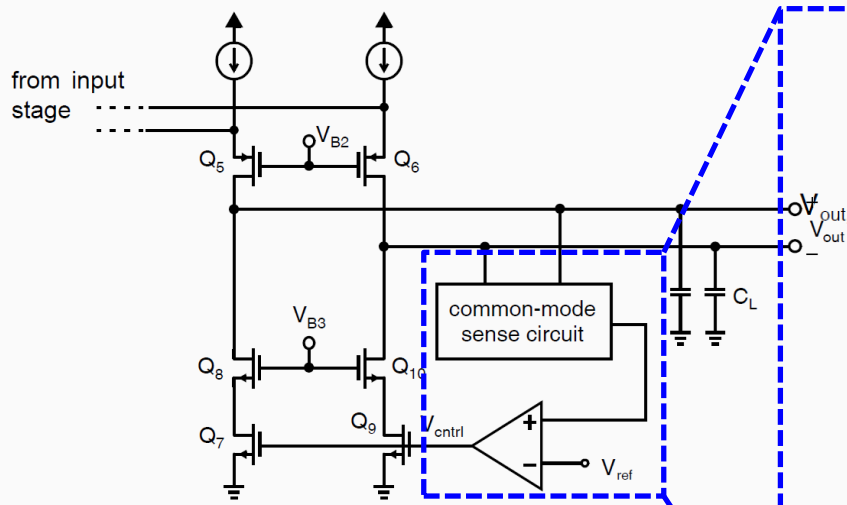


Fig. 6.37 The common-mode feedback loop in a fully differential folded-cascode opamp.

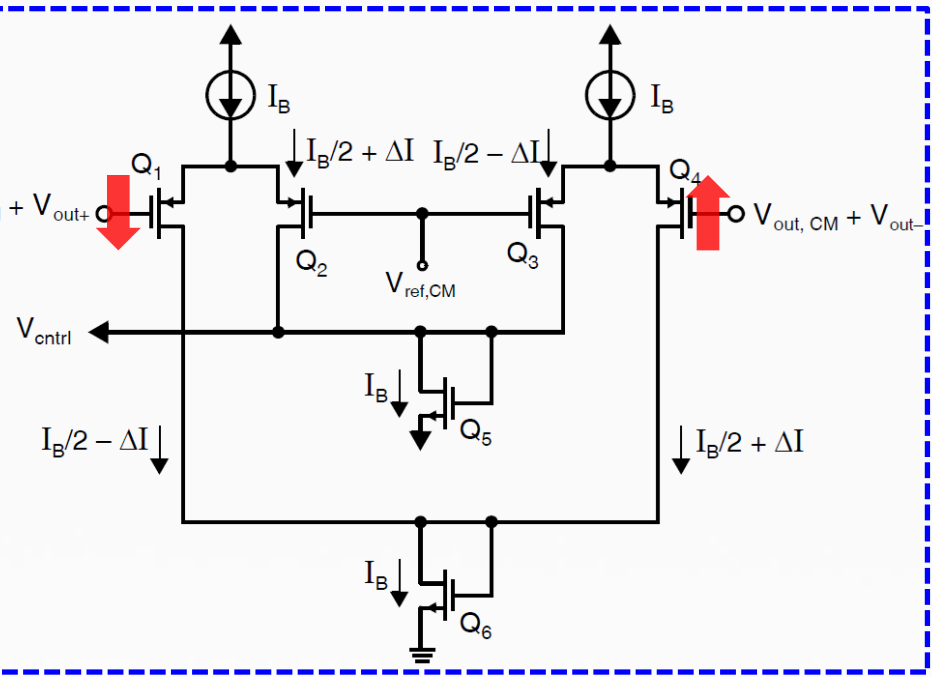


Fig. 6.34 An example of a continuous-time CMFB circuit

Three operations of CMFB

1. Sensing the output CM level
2. Comparison with a reference
3. Returning the error to the amplifier's bias network



Concept of CMFB

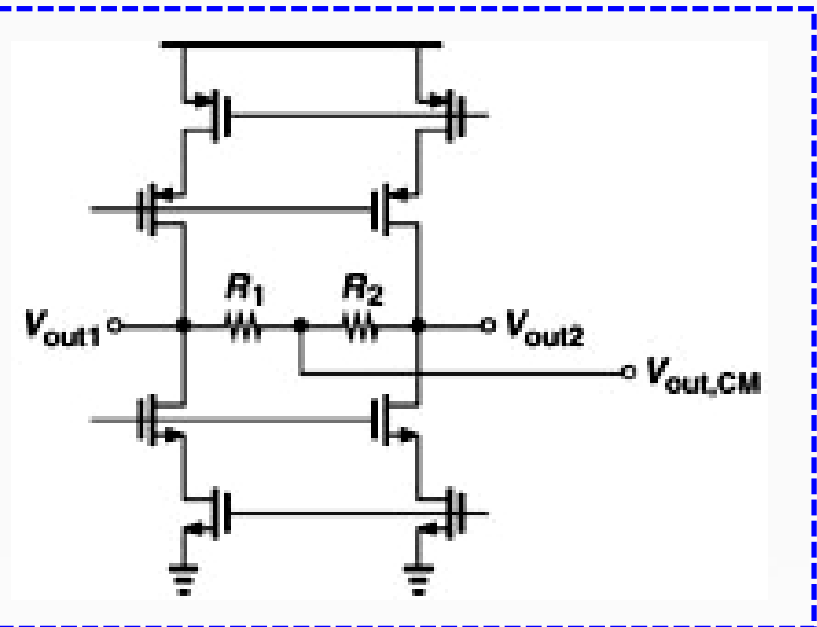
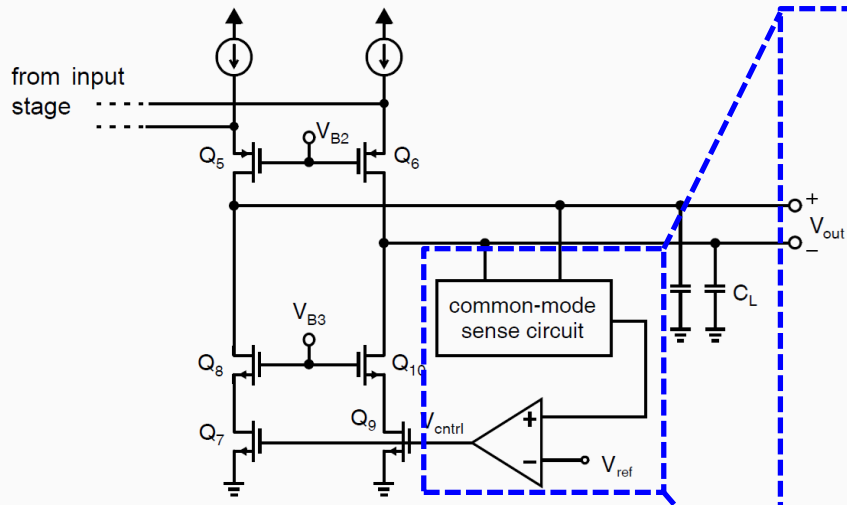


Fig. 6.37 The common-mode feedback loop in a fully differential folded-cascode opamp

Resistive sensing CMFB



Set CM level easily



Large area and suffer from parasitic capacitance.

(if $R_1=R_2$)

$R_1, R_2 \gg R_{out}$

(To avoid lowering the open loop gain.) 17

