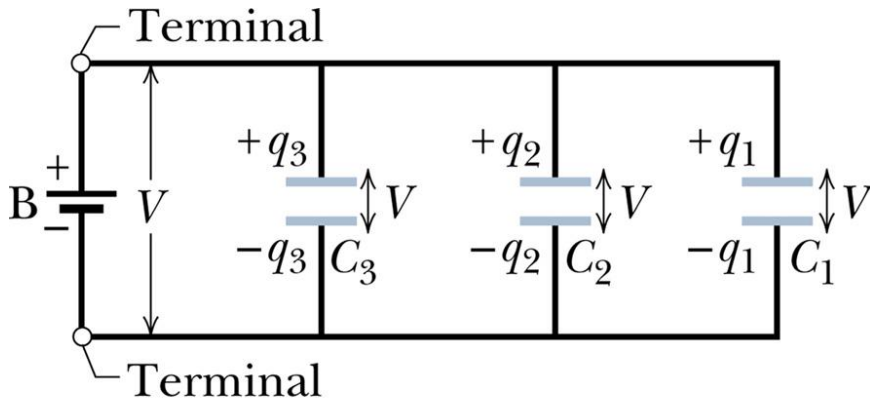


# Copyright statement

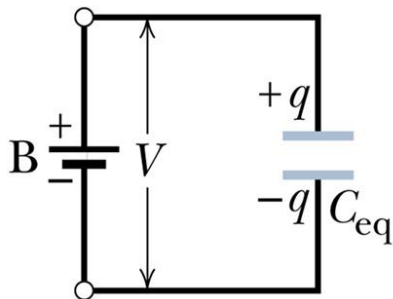
- The images and the pictures in this lecture are provided by the CDs accompanied by the books
  1. University Physics, Bauer and Westfall, McGraw-Hill, 2011.
  2. Principles of Physics, Halliday, Resnick, and Walker, Wiley, 8<sup>th</sup> and 9<sup>th</sup> Ed.
- The rest is made by me.

# Capacitors in parallel



(a)

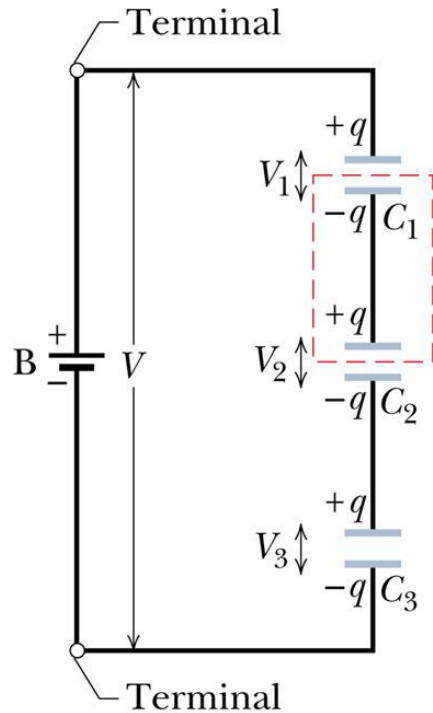
$$C_{\text{eq}} = \frac{q}{V} = C_1 + C_2 + C_3$$



(b)

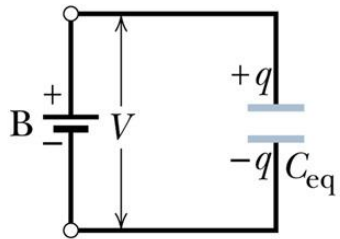
n 개가 연결된 경우 
$$C_{\text{eq}} = \sum_{i=1}^n C_i$$

# Capacitors in series



(a)

$$\frac{1}{C_{\text{eq}}} = \frac{q}{V} = \frac{1}{C_1} + \frac{1}{C_2} + \frac{1}{C_3}$$

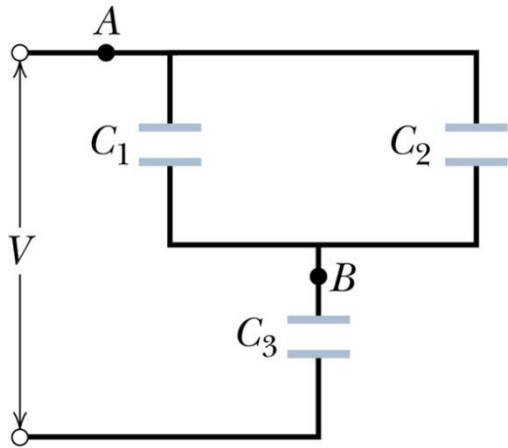


(b)

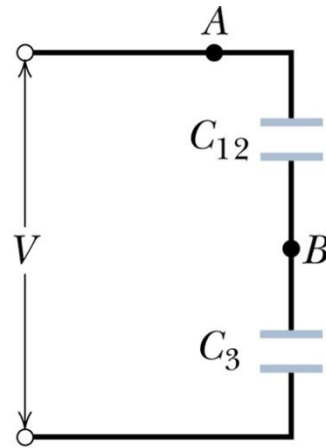
n 개가 연결된 경우

$$\frac{1}{C_{\text{eq}}} = \sum_{i=1}^n \frac{1}{C_i}$$

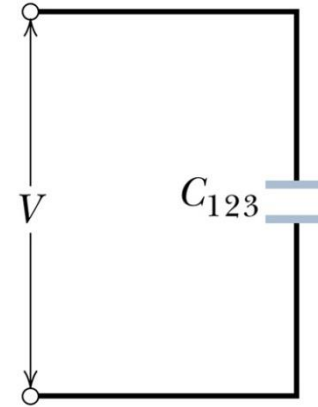
# Example 1



(a)

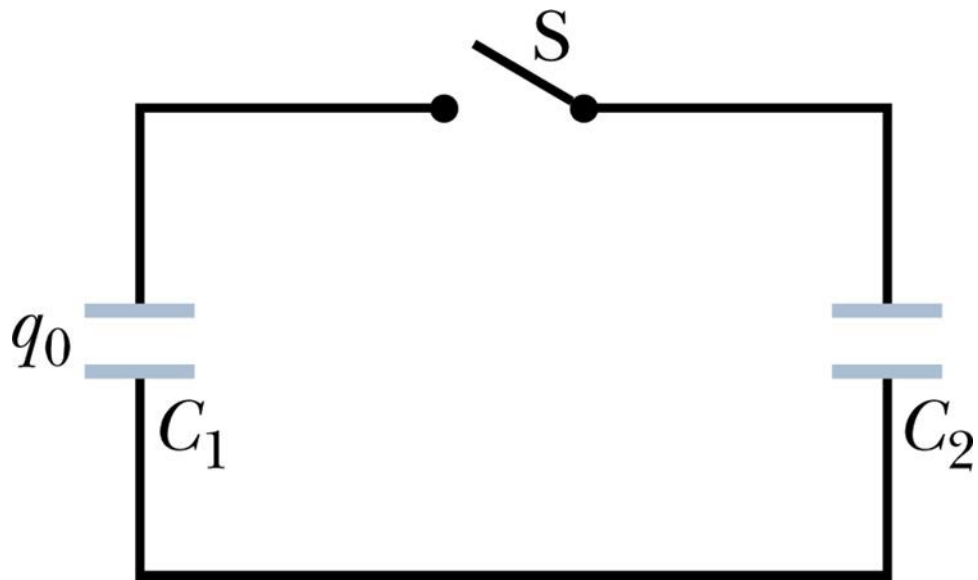


(b)

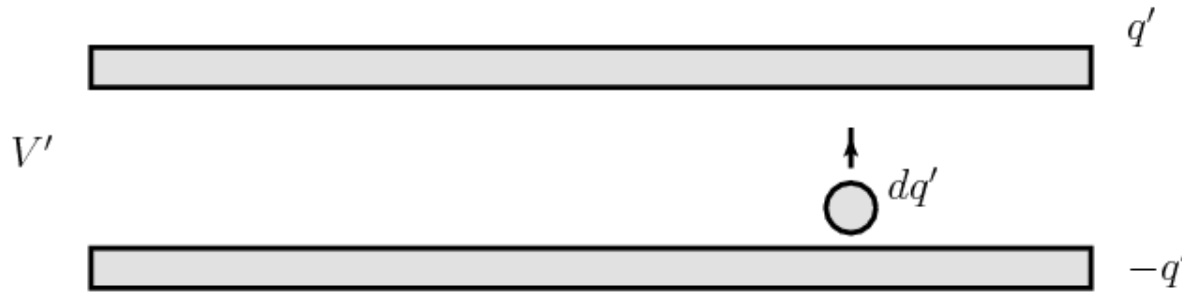


(c)

# Example 2



# Energy stored in electric field



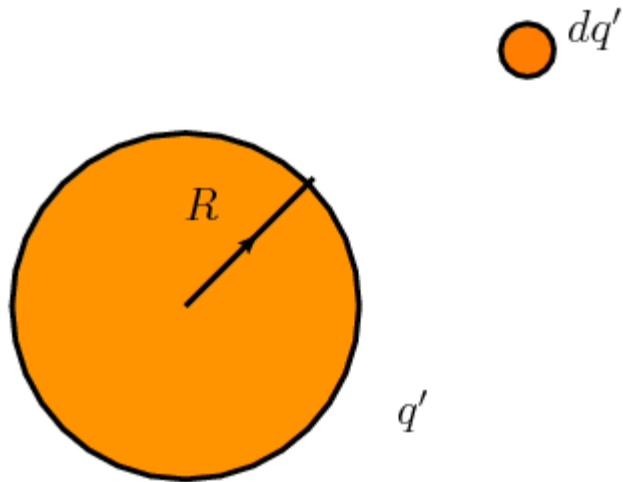
축전기의 전하를 0에서  $q$ 까지 만들 때 들어가는 일

축전기에 저장된 전기에너지와 전기에너지 밀도

$$U = \frac{q^2}{2C} = \frac{1}{2}CV^2$$

$$u = \frac{1}{2}\epsilon_0 E^2$$

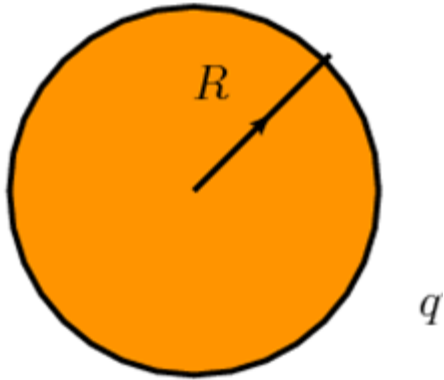
# 보기문제 25-5



$$U = \frac{q^2}{8\pi\epsilon_0 R}$$

$$u = \frac{q^2}{32\pi^2\epsilon_0 R^4}$$

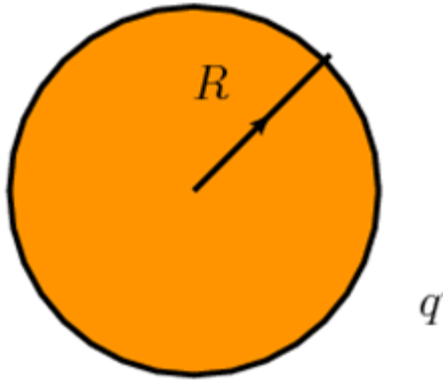
# Electric energy of a charged sphere



$$U = \frac{q^2}{8\pi\epsilon_0 R}$$

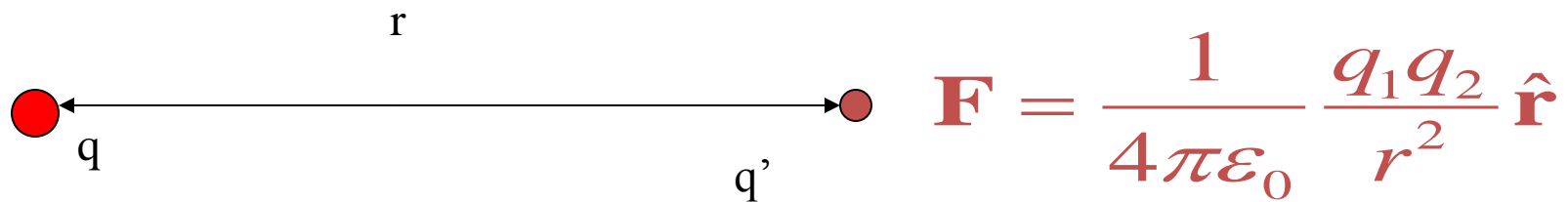


# Charged sphere as a capacitor

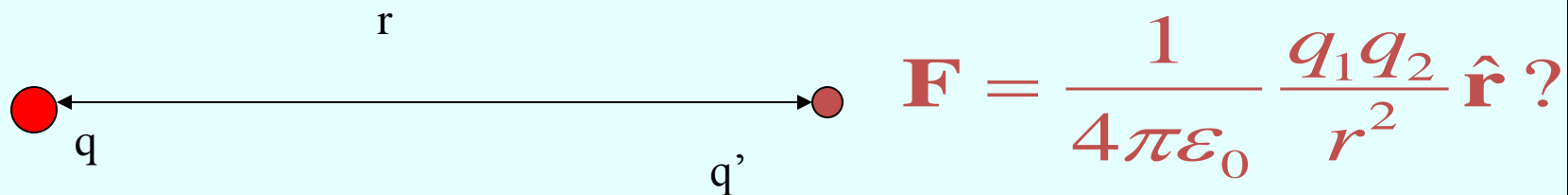


$$C = 4\pi\epsilon_0 R$$

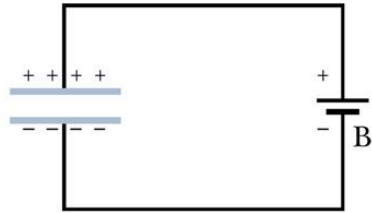
$$U = \frac{q^2}{8\pi\epsilon_0 R}$$



Dielectric material



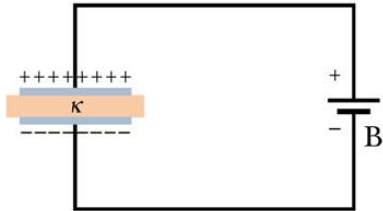
# Capacitor with dielectric material



$$C = \epsilon_0 \mathcal{L} \longrightarrow \kappa \epsilon_0 \mathcal{L} = \kappa C_{\text{air}}$$

Point charge in dielectric material

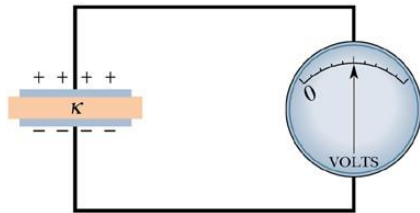
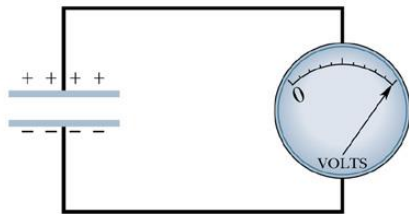
$$E = \frac{1}{4\pi\kappa\epsilon_0} \frac{q}{r^2}$$



(a)  $V = \text{a constant}$

Electric field of an isolated charged surface inside dielectric material

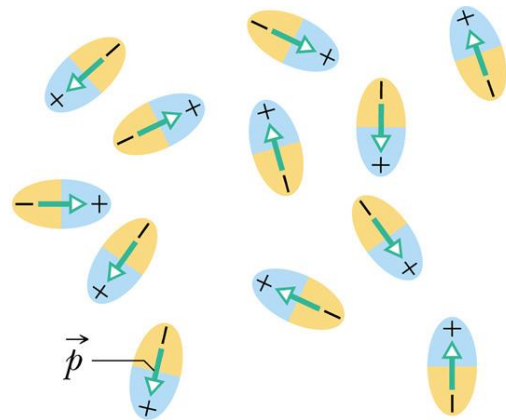
$$E = \frac{\sigma}{\kappa\epsilon_0}$$



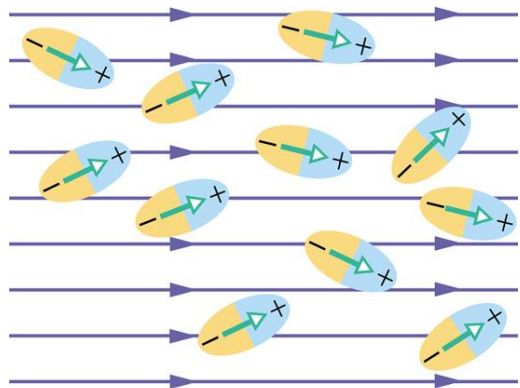
(b)  $q = \text{a constant}$

# Dielectric material: atomic view

Polar dielectric material

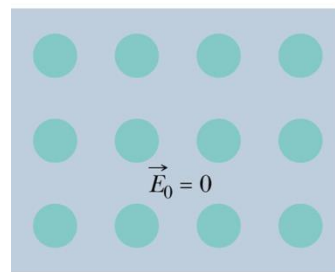


(a)

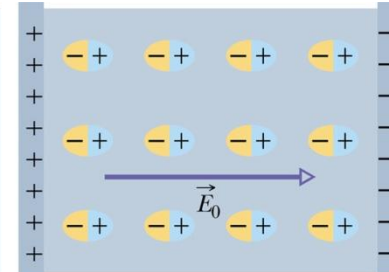


(b)

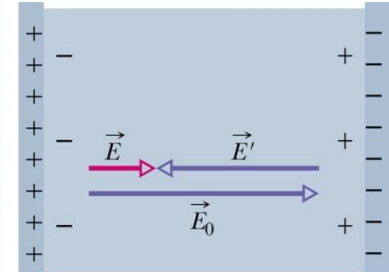
Nonpolar dielectric material



(a)

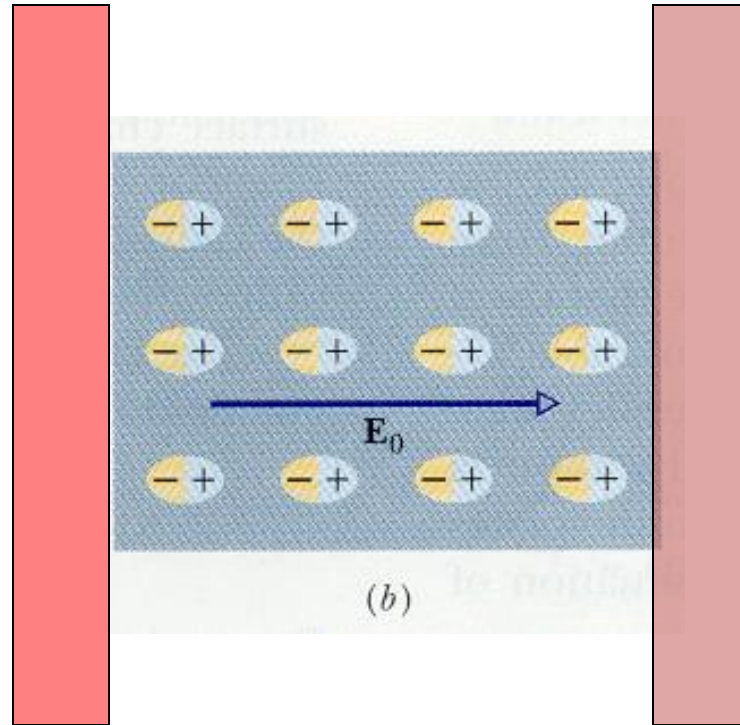


(b)



(c)

# Effect of aligned dielectric on E

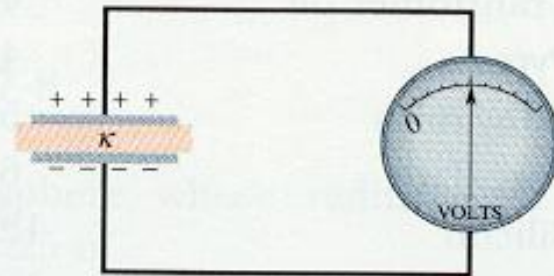


$$E < E_0$$

$$E_0 / E = \kappa \text{ with } \kappa > 1$$

여기서  $\kappa$ 를 유전상수 (dielectric constant)라고 한다.

# Dielectric material and capacitors



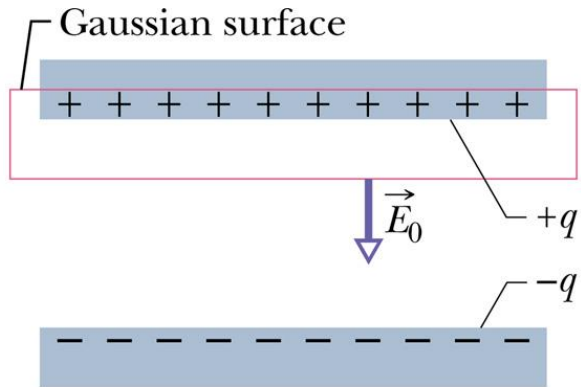
$q = \text{a constant}$

(b)

Q 일정  
V 감소

$$C \left( = \frac{q}{V} \right) = \kappa C_0 \quad (\kappa > 1)$$

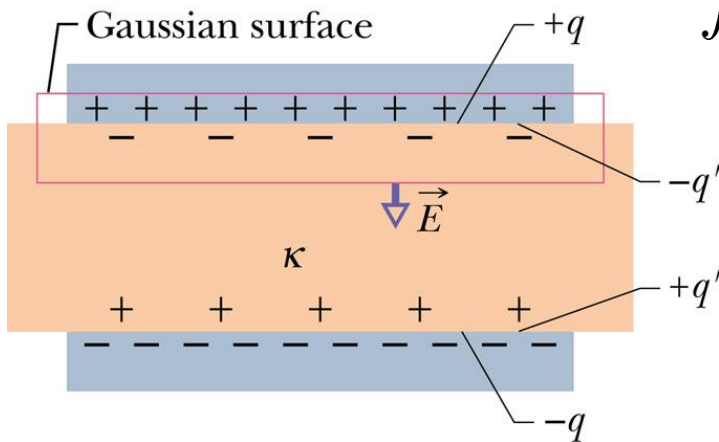
# Dielectric material and Gauss law



(a)

$$\epsilon_0 \oint \vec{E} \cdot d\vec{A} = \epsilon_0 E_0 A = q$$

$$E_0 = \frac{q}{\epsilon_0 A}$$



(b)

$$\epsilon_0 \oint \vec{E} \cdot d\vec{A} = \epsilon_0 E A = q - q' \quad E = \frac{q - q'}{\epsilon_0 A}$$

$$E = \frac{E_0}{\kappa} = \frac{q}{\kappa \epsilon_0 A} \quad q - q' = \frac{q}{\kappa}$$

$$\epsilon_0 \oint \kappa \vec{E} \cdot d\vec{A} = q$$

Free charge

# 진공과 유전체에서의 전기현상의 차이

Coulomb force

$$\mathbf{f} (2 \leftarrow 1) = \frac{1}{4\pi\epsilon_0} \frac{q_1 q_2 (\mathbf{r}_2 - \mathbf{r}_1)}{|\mathbf{r}_2 - \mathbf{r}_1|^3}$$

$$\mathbf{f}_c = \frac{1}{4\pi\kappa\epsilon_0} \frac{q_1 q_2 (\mathbf{r}_2 - \mathbf{r}_1)}{|\mathbf{r}_2 - \mathbf{r}_1|^3}$$

Electric field

$$\mathbf{E}(\mathbf{r}) = \frac{1}{4\pi\epsilon_0} \frac{q \mathbf{r}}{r^3}$$

$$\mathbf{E}(\mathbf{r}) = \frac{1}{4\pi\kappa\epsilon_0} \frac{q \mathbf{r}}{r^3}$$



Gauss law

$$q / \varepsilon_0 = \oint \mathbf{E} \cdot d\mathbf{A}$$

$$q / \kappa \varepsilon_0 = \oint \mathbf{E} \cdot d\mathbf{A}$$

parallel plate capacitor

$$C = \varepsilon_0 \frac{A}{d}$$

$$C = \kappa \varepsilon_0 \frac{A}{d}$$

electric field energy density

$$u = \frac{1}{2} \varepsilon_0 E^2$$

$$u = \frac{1}{2} \kappa \varepsilon_0 E^2$$

# Capacitor connection 1

